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## A computer program for determining Hinshelwood rate mechanisms from nonisothermal pellet data

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A COMPUTER PROGRAM FOR DETERMINING

"HINSHELWOOD RATE MECHANISMS

FROM

NONISOTHERMAL PELLET DATA"

BY

JOSEPH J. ATKINS

A THESIS

PRESENTED IN PARTIAL FULFILLMENT OF

THE REQUIREMENTS FOR THE DEGREE

OF

MASTER OF SCIENCE IN CHEMICAL ENGINEERING

AT

NEWARK COLLEGE OF ENGINEERING

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Newark, New Jersey

1969

## ABSTRACT

Methods of determining Hinshelwood rate correlations from non isothermal catalyst data was studied. It was determined for any chemical system involving a reacting gas mixture over a porous catalyst a node analysis could be used to determine chemical concentration and temperature variation through the pellet. Calculation performed with a spectra 360/Fortran 4 program defined the Hinshelwood equation from estimated surface rates. Then utilizing node analysis to determine concentration and temperature variance, transport and rate equations were integrated through the pellet to obtain a total pellet rate of reaction. For acceptance of Hinshelwood equations the calculated total rate must equal the measured total rate and the Hinshelwood constants must meet the Hinshelwood acceptance criteria. A sample problem employing Hydrogen and Oxygen catalyzed over platinum was used for checkout.

APPROVAL OF THESIS  
A COMPUTER PROGRAM TO DETERMINE  
HINSHELWOOD MECHANISMS  
FROM NON ISOTHERMAL PELLET DATA  
BY  
JOSEPH J. ATKINS  
FOR  
DEPARTMENT OF CHEMICAL ENGINEERING

BY

FACULTY COMMITTEE

APPROVED: \_\_\_\_\_  
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NEWARK, NEW JERSEY

JUNE, 1969

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## NOMENCLATURE LIST

|                                   |  |
|-----------------------------------|--|
| AR or S                           | Mean transport area and AR is mean area between nodes                  |
| C <sub>A</sub> or C <sub>S</sub>  | Concentration of components A through S                                |
| DEA or DES                        | Diffusivities of components A through S                                |
| DR or $\Delta X$                  | Distance between nodes   |
| E                                 | Pellet effectiveness   |
| F                                 | Feed rate  |
| $\Delta H$                        | Heat of reaction   |
| L <sub>o</sub>                    | Total number of adsorption sites                                       |
| K <sub>1</sub> and K <sub>2</sub> | Forward and reverse rate constants                                     |
| KE                                | Equilibrium constant   |
| K <sub>1</sub> to K <sub>5</sub>  | Hinshelwood constants  |
| k or cK                           | Thermal conductivity   |
| N                                 | Node number  |
| P <sub>A</sub> or P <sub>S</sub>  | Partial pressure of components A through S                             |
| POT                               | Potential term in Hinshelwood equation                                 |
| RA                                | Diffusion rate   |
| R(N)                              | Node rate reduced to meet equation and diffusion limits                |
| R <sub>T</sub>                    | Total pellet reaction rate   |
| r                                 | Reaction rate  |
| R                                 | Pellet radius  |
| X, X <sup>1</sup>                 | (X) conversion X <sup>1</sup> amount of component adsorbed on catalyst |
| ZD                                | Multiplier for adjusting surface rate estimate                         |
|                                   | Number of adsorption sites used by a component                         |
|                                   | Density  |

## I

INTRODUCTION

A topic of significant interest in the field of catalyst research is the application of computer techniques to determine Langmuir Hinshelwood Rate Mechanisms as applied to the design of catalytic reactors. Hinshelwood Rate Mechanisms are defined by the rate equation which best fits experimental reactor data. The rate forms are all based on the assumption that one reaction step controls the reaction rate and that a linear Langmuir isotherm for adsorption of reactant is descriptive of the chemical reaction being studied.

A comprehensive review of the available literature in this area and the work done by previous investigators revealed that Hinshelwood rate equations determined to date have been primarily based upon experimental data using fine particle catalyst. This was apparently because the influence of temperature and concentration variation associated with fine particles is small thus minimizing errors in the results. In commercial chemical production plants, however, catalysts are generally in pellet form and such catalyst structures do encounter significant variations in temperature and chemical concentration.

From these considerations, the question arose whether the Hinshelwood rate equations based upon the fine particle catalyst data were valid for other pellet geometry, catalyst properties and flow conditions.

It was hypothesized that the errors introduced by the change in geometry might be reduced if the pellet data could, by some method, be analyzed directly to determine the catalytic mechanisms. The object of the work undertaken therefore, was to establish a means of determining Hinshelwood equations directly from pellet data.

The method developed estimated Hinshelwood rate equations from reactor pellet data. The process encompassed estimating surface rates, and then integration of the transport equations through the pellet to arrive at a total rate which agreed with catalyst total rates determined experimentally.

Node analysis was selected for integration of the transport equations. A computer program was assembled and sample problems examined via this form of analysis. One such sample encompassed several computer runs for Hydrogen-Oxygen Catalysis over platinum summarized at the end of this discussion. Discussion of program input and nomenclature is presented in the Appendix.

## II

### DISCUSSION OF ANALYSIS

#### A. Catalyst Reactions

A review of reaction rate controls indicated that a catalyst will not make a reaction proceed between chemical species that would not proceed in its absence, but it can increase reaction rates. The catalyst property promoting reaction rate is conjectured (5) to be chemisorption of gas or liquid on the catalyst surface producing an activated complex. The gas to catalyst complex is unstable and requires less energy for reaction to occur than is needed for reaction of the gas as without a catalyst. The change in the path of the chemical reaction sequence along with the accompanying decrease in energy requirement per step leads to greater chance of chemical reaction upon gas to catalyst contact. Interest in catalysts therefore, relates to the effect they have on the reaction rate. For purposes of analysis, one transport or reaction step is assumed to control. If the chemist is to determine a representative rate equation for catalyst data, he needs to know which of the following mechanisms is controlling.

#### Types of Rate Controlling Mechanisms

1. Mass transfer from the mainstream to and from the solid surface.
2. Diffusion of chemical species into and out of the catalyst pore structure.
3. Activated adsorption of reactants and desorption of products.
4. Speed of reaction of the adsorbed species on the catalyst.

For establishing a method of determining Hinshelwood mechanism from porous catalyst data, it is of major importance that the effect of each controlling mechanism or catalyst reaction be obtained. Then in the process of integrating the rates through the pellet, all factors will be accounted for providing the means for defining both the rate controlling step and estimating total pellet reaction rate. The representative rate equation should be based upon rates defined by reaction kinetics, unaltered by transport phenomena. Each of the four rate steps or mechanisms mentioned are considered in brief as follows.

1. Main stream to pellet transport. The Type 1 rate control -mainstream to pellet- limits the rate of reaction by failure of reactant to diffuse rapidly enough to the pellet surface to feed the reaction. This results from film formation over the catalyst, decreasing the diffusion rate of the reactant. If the main stream flow over the surfaces is high, films are swept away. Careful control of reactor flow conditions will make these effects negligible and minimize their influence on catalytic reaction rate. The influence of the variation of surface concentrations produced during transport of reactant from the main stream to the pellet is small as long as pellet pore diffusion effects observed are small. If variation caused by pore diffusion should be large, then surface concentration should be adjusted to account for effect of transport from the main stream.

2. Pellet diffusion. The Type 2 rate control -pellet diffusion- is incurred by chemical diffusion limiting the flow into the catalyst pores. The diffusion effect upon reaction rate is analytically deter-

minable by integrating the mass transport equations through the porous material. Reaction rates may be estimated from the concentration versus pellet location relationship. If diffusion limits are severe, the reaction rate may further be limited by the inability of the species to penetrate the pore structure or for the product to escape fast enough, preventing the feeding of the reaction.

For development of the analytical approach (8) integration of transport equations is accomplished in the following manner. It is assumed that the catalyst is in the shape of a sphere and that the diffusion of the reactant "A" of partial pressure  $P$  is diffusing through a thin spherical shell of thickness  $\Delta R$ . The difference between the amount of reactant diffusing into the shell,  $N_{A/in}$ , and the amount exiting from the shell,  $N_{A/out}$ , equals the amount depleted by the reaction in the shell.

$$N_{A/in} - N_{A/out} = \int S \bar{r} \Delta R \quad (1)$$

The mass flux is equal to the product of the effective diffusivity for porous catalyst ( $D_A$ ) and the concentration or partial pressure drop ( $dp/dr$ ) across the shell. Substitution for  $N_A$  gives us the following result:

$$D_A \frac{\partial P_A}{\partial R} / \partial R / in - D_A \frac{\partial P_A}{\partial R} / \partial R / out = \int S \bar{r} \Delta R \quad (2)$$

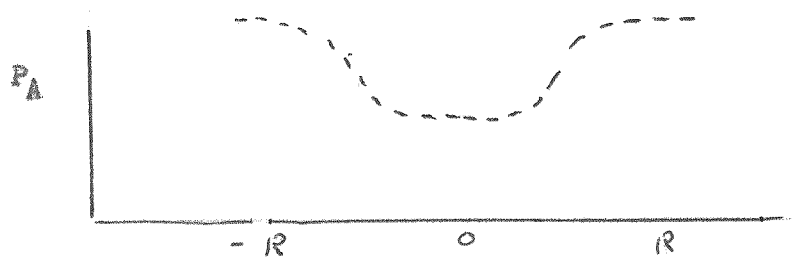
$$\frac{\partial}{\partial R} (D_A P_A / \partial R) - \int S \bar{r} = 0$$

The above equation may be solved if rate  $r$  is first order with respect to partial pressure of "A" (KPA). The equation is then of the form as follows:

$$\frac{\partial}{\partial R} \left( P_A \frac{\partial}{\partial R} \right) - \left( \frac{PSk_1}{D_A} \right) P_A = 0 \quad (3)$$



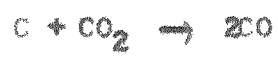
The term  $\frac{PSK}{D \hat{h}^2}$  has been arbitrarily set equal to the square of the Thiele modulus  $\hat{h}^2$ . Integration of the differential equation provides the partial pressure curve through the pellet as a function of radius.



For estimating the rate of reaction in single pellets, the transport equations have been solved using first order rate approximation of the data. When the total pellet rate is determined, it is divided by the rate for the same volume of catalyst unaffected by diffusion, obtaining a pellet effectiveness ( $\epsilon$ ). Effectiveness is plotted against Thiele modulus for first order reactions, thus rates can be determined from these effectiveness plots for any given values of the modulus.

Estimating pellet rates becomes more complex if the rate equation is not a first order approximation. Since all Hinshelwood rate equations are more complex, it is the latter case in which we have the greatest interest.

An example problem illustrates methods of solving for pellet concentrations and rates. Analysis of carbon and carbon dioxide catalysis was performed by Austin and Walker (8). The reaction of carbon dioxide to form carbon monoxide is written as follows:



Small amounts of carbon monoxide inhibit this reaction. Thus, diffusion of the carbon monoxide out as well as carbon dioxide into the catalyst must be considered. It was ascertained beforehand that a Hinshelwood rate equation represented the rate data:

$$r = K P_A / (1 + K_2 * P_A + K_3 * P_B) \quad (4)$$

Considering the mass transport equation for carbon dioxide  $P_A$  and carbon monoxide  $P_B$ , we obtain transport equations for  $CO_2$  and  $CO$ :

1.) carbon dioxide ( $CO_2$ )

$$\frac{\partial}{\partial R} (D_A \frac{\partial P_A}{\partial R}) - \beta S \left[ \frac{K_1 * P_A}{1 + K_2 * P_A + K_3 * P_B} \right] = 0 \quad (5)$$

2.) carbon monoxide ( $CO$ )

$$\frac{\partial}{\partial R} (D_B \frac{\partial P_B}{\partial R}) - 2 \beta S \left[ \frac{K_1 * P_A}{1 + K_2 * P_A + K_3 * P_B} \right] = 0 \quad (6)$$

Multiplying equation (1) by  $\frac{P_A}{2}$  and equation (2) by  $P_A$  and subtracting 3 from 1 we get the following:

$$\frac{\partial}{\partial R} (D_A \frac{\partial P_A}{\partial R}) = -\frac{1}{2} \frac{\partial}{\partial R} [D_B \frac{\partial P_B}{\partial R}] \quad (7)$$

Integration occurs in two steps, and in each case  $R$  is the independent variable.

Step 1 Integration Yields the following:

$$D_A \frac{\partial P_A}{\partial R} = -\frac{1}{2} D_B \frac{\partial P_B}{\partial R} + C \quad (8)$$

Solving for  $C$  we note the condition at pellet center where mass flux is zero.

$$R = 0 \quad \frac{\partial P_A}{\partial R} = 0 \quad \frac{\partial P_B}{\partial R} = 0$$

Step 2 Setting C = 0

$$D \partial P_A / \partial R = -1/2 D_B \partial P_B / \partial R \tag{10}$$

Again integrating the partial pressures with respect to R we get the following:

$$D_A P_A = -1/2 D_B P_B + C \tag{11}$$

We make use of the second boundary condition that the partial pressures at the pellet surface are the stream conditions.

$$R = R \quad P_A = P_{AO} \quad P_B = P_{BO} \tag{12}$$

$$C = D_A P_{AO} + 1/2 D_B P_{BO}$$

Substituting and refining the equation, we get the following:

$$P_B = 2 D_A / D_B (P_{AO} - P_A) + P_{BO} \tag{13}$$

The authors integrated the equation assuming P<sub>BO</sub> of carbon monoxide is zero at the surface and substituting back into the initial transport equation containing partial pressure (P<sub>A</sub>) as a function of radius.

(14)

$$\partial / \partial R (D_A \partial P_A / \partial R) - \int \int (K_1 * P_A / (1 + K_2 * P_A + K_3 * D_A / D_B (P_A - P_{AO}))) = 0$$

It is worthy of note that the transport equations for diffusion of each chemical specie are interrelated by the chemical mass balance. Also, the conditions of known surface concentrations and zero diffusion rate at pellet center are influential in node analysis. Node analyses are described (3) as used in determining temperatures of materials at specific locations called nodes.

The Austin-Walker example considers two chemical components. If these analyses are extended to consider a reaction of the type  $(A + B \rightarrow R + S)$ , the four chemical species require four mass transport equations. Temperature variation through the catalyst provides a fifth. Because of the large number of partial differential equations involved, a node analysis was selected for determination of Hinshelwood rate equations for non-isothermal pellet data.

3. Adsorption and desorption. The Type 3 rate control - adsorption and desorption - occurs when the speed of reaction is limited by the rate of adsorption and desorption of chemical species. It is noted (4) that the concentration (X) of chemical species adsorbed on a solid surface is related to the partial pressure of "A" in the main stream. This relation is defined as the Langmuir Isotherm.

$$X = a (P_A)^n \tag{15}$$

For adsorption rates or condensation on the catalyst surface, rate is assumed proportional to the partial pressure of "A". This is based upon kinetic theory of gases where the reaction is controlled by the number of molecular collisions molecule "A" makes with the catalyst surface. Rate of adsorption =  $K_1 P_A (1 - \sigma)$ . Here  $\sigma$  is the surface covered with reactant or product, and a linear isotherm ( $n = 1$ ) has been assumed. Desorption on the other hand is a function of the product of a constant and the concentration of the adsorbed product.

The desorption rate is defined as follows:

$$\text{Rate of Desorption} = K_2 \sigma$$

At equilibrium condensation rate equals evaporation rate.

$$K_1 P_A (1 - \sigma) = K_2 \sigma'$$

$$\sigma = K_1 * P_A / (K_2 + K_1 * P_A) \quad (16)$$

Further development involved study of more than one chemical species vying for the same site. Parameters  $\sigma$  and  $\sigma'$  are the coverage of metal surface by species A and B, respectively. Then  $(1 - \sigma - \sigma')$  is the uncovered catalyst surface.

$$\text{Condensing rate of A} = K_1 (1 - \sigma - \sigma') P_A \quad (17)$$

$$\text{Evaporation rate} = K_2 \sigma \quad (18)$$

A similar equation for species B can also be defined.

$$K_1' P_B (1 - \sigma - \sigma') = K_2' \sigma'$$

The catalyst surface coverage of component B, ( $\sigma'$ ) may now be obtained from the two equations for species A and B if we assume that the slow step is the adsorbing of "A". Thus surface coverage of "A"  $\sigma$ , is negligible and influences the reaction very little. Solving the above equations for  $\sigma'$  we obtain the following:

$$\sigma' = K_1' P_B \left[ \frac{1}{K_2' + K_1' P_B} \right] \quad (19)$$

The rate of reaction of "A" is the product of the free surface  $(1 - \sigma - \sigma')$  and the specific rate of adsorption of "A" per unit free surface, or the rate of reaction of A proportional to a constant times partial pressure

of species "A" upon the free adsorption sites ( $\sigma = 0$ ).

$$r = KP_A (1 - \sigma^0)$$

$$r = K K_2^0 \left( \frac{1}{K_2^0 + K_1^0 P_B} \right) P_A \quad (20)$$

This is the form of one Hinshelwood equation. Other equations may be determined by assuming adsorption of B or desorption of products R and S control.

4. Surface reaction. The Type 4 rate control surface reaction is associated with the speed of the reaction on the catalyst surface. Concentrations of the chemisorbed reactant are controlled by the adsorption equilibrium between fluid and solid while the surface rate is a function of the surface adsorbed reactants and vacant site locations. In the case of a monomolecular reaction (5).



The chemical reaction is defined by the following equation:

$$r = K_1 (P_A - P_B/KE) \quad (21)$$

If the reaction rate is controlling, the adsorption steps are assumed to be in equilibrium between condensation and evaporation of reactants and products. Surface concentrations of A and R can then be determined from Langmuir isotherm considerations. It is noted for specie "A" in the previous section, the following equation was defined.

$$C_A = \sigma = K * P_A / (1 + K * P_A) \quad (22)$$

It is further noted that for equilibrium condition in a reaction, the equilibrium constant is defined as the ratio of the forward rate constant divided by the reverse rate constant.

$$K_1 (1 - \sigma) P_A = K_2 \sigma$$

$$K = K_1/K_2 = \sigma/(1 - \sigma) P_A \quad (23)$$

If component "A" is in an admixture with several other components A, B and R adsorbed on active sites, adsorption equilibrium equations may be written for each component. Available free sites will equal to the total number of sites less those sites ( $C_A \dots C_R$ ) used by the components

$$C_L = (1 - \sigma) = L - (C_A + C_R) \quad (24)$$

Concentrations  $C_A$  and  $C_R$  are defined by equation 22 where the concentration is the product of the equilibrium constant, the number of free sites, and the activity or partial pressure of the component ( $C_A = K(1 - \sigma)P_A$ ). The concentration of free sites may then be defined as follows:

$$C_L = L / (K (1 - \sigma) P_A + K_R (1 - \sigma) P_R) \quad (25)$$

Since  $C_L$  EQUALS  $L - \sigma$  we solve for  $C_L$  arriving at equation

$$C_L = L / (1 + K_A * P_A + K_R * P_R) \quad (26)$$

The equilibrium concentration of "A" on the catalyst surface is obtained by substituting for  $C_L$  or  $(1 - \sigma)$  in equation  $C_A = K(1 - \sigma) P_A$ .

$$C_A = K_A ( L / (1 + K_A * P_A + K_R * P_R) ) P_A \quad (27)$$

and for the product concentration  $C_R$

$$C_R = K_R ( L / (K_A * P_A + K_R * P_R) ) P_R \quad (28)$$

Making substitutions for  $C_A$  and  $C_R$  in the rate equation we obtain

$$\bar{r} = k_1 \left( L / (K_A * P_A + K_R * P_R) \right) \left( K_A * P_A - \frac{K_R * P_R}{KE} \right) \quad (29)$$

Additional equations have been derived assuming different surface rate steps controlling the bulk of which are known as Hinshelwood rate equations. A least square approximation of the rate constants is used to derive an equation representative of the rate versus concentration data. The equation best fitting the data is considered representative and because the equation is based upon a specific rate controlling step, the controlling mechanism is identified.



### B. Hinshelwood Rate Equation Determination

The previous section discussed the control mechanisms and how the nature of these mechanisms affect the derivation of Hinshelwood equations. It was found that catalysis is composed of a sequence of reaction steps; and for analysis one step is assumed to control the overall rate. To pin point the controlling step the rate equation is determined for a reaction  $A + B \rightarrow R + S$  the general rate equation as defined in (9) is:

$$r = \frac{K (P_A * P_B) - (P_R * P_S)/K_E}{(1 + K_2' * P_A + K_3' * P_B + K_4' * P_R + K_5' * P_S)^n} \quad (30)$$

The Hinshelwood rate constants are then  $K$ ,  $K_2'$ ,  $K_3'$ ,  $K_4'$ , and  $K_5'$ . To determine these constants from rate data the equation is rewritten with all the unknown constants to one side of the equation.

$$K_1 + K_2 * P_A + K_3 * P_B + K_4 * P_R + K_5 * P_S = \left[ \frac{POT}{r} \right]^{1/n} \quad (31)$$

Solution of these constants is accomplished via least square linear approximation. Recent studies show non linear analysis to be more accurate for rate correlation but, here it was not needed to demonstrate methods of estimating constants from pellet information. The linear least square analysis assumes various rate equations and solves for values of  $K_1$ , through  $K_5$  using rate ( $r$ ) and concentration data  $P_A$ ,  $P_B$ ,  $P_R$ , and  $P_S$ . As an example, let us consider the rate equation for adsorption of "A" controlling. Large equilibrium constant makes the second term of numerator negligible.

$$r = P_A * P_B / (1 + K_3' * P_B + K_4' * P_R + K_5' * P_S)^n \quad (32)$$

Placing all rate constants on one side of the equation we obtain the rate for  $(K_1 + K_3 * P_B + K_4 * P_R + K_5 * P_S) = K * P_A * P_B / r$ . For the results of the least square analysis to be acceptable the terms  $K_1$ ,  $K_3$ ,  $K_4$ , and  $K_5$  must all be positive or zero otherwise equilibrium constant (forward and reverse rate) must be of opposite sign and cannot be equal as required for equilibrium. And since  $P_A$  does not appear in the denominator the constant  $K_2$  must be zero. In similar manner, a large number of reactions are tried until all constants are positive or zero. When all the constants meet these requirements, the equation is found acceptable. Of the acceptable equations, the equation which shows the least deviation of the calculated rate from the measured rate is generally selected.

### C. Reactor Pellet Data Analysis

The rate data itself is of importance to the analysis. Since results of Hinshelwood analyses are sensitive to errors introduced by the data, it is desirable to measure rates in a reactor segment where little change in physical conditions occur and chemical changes are readily measured. The two principal types of reactors used to measure rates are the differential and integral reactors.

The differential reactor is of interest because chemical reaction is performed in short reactor sections where conditions of temperature and stream chemical composition can be held constant. The reacting mixture is cycled through the reactor and the change in chemical composition noted. The rate of reaction in this increment of volume is defined (5) by an equation relating the changes in feed composition ( $F\Delta X$ ) to the rate of reaction ( $r$ ) in the small increment of catalyst mass ( $\Delta w$ ):

$$F \Delta X = \bar{r} \Delta W \quad (33)$$

Integral data is obtained from reactors where temperature and concentration vary. To determine reactor size integration of the equation 31 provides a relation between reactor weight catalyst, the feed rate  $F$ , and the amount of reaction ( $\Delta X$ ) occurring in the reactor bed,

$$F/W = \int dX/r \quad (34)$$

Integral data is plotted in terms of conversion  $X$  versus  $W/F$ . Thus for a given conversion it is possible to take the value of  $W/F$  and size the reactor for a given feed rate. Rates are determined by taking the slope of the plot ( $\Delta X/\Delta W/F$ ); this provides a result similar to differential rate equation 31.

#### D. Node Analyses

The approach to determining Hinshelwood mechanisms from non-isothermal pellet data employs a node analysis similar to that used in Southwell's Relaxation Method. In Southwell's method (3) for heat transfer, nodes are specified geometric locations distributed uniformly throughout the material. Temperature gradients are calculated from node to node based upon known boundary temperatures, known material thermal properties and known fact that the sum of the heat fluxes into each node must be zero for steady state temperature.

The heat fluxes are determined from node to node based upon the Fourier equation -  $q = \frac{(KA)}{x} (T_{\text{node } 2} - T_{\text{node } 1}) = c' (T_{N2} - T_{N1})$ . (35)

Heat fluxes into and out of the nodes are summed with positive values for heat flux in, and negative for heat flux out. The sums of the heat fluxes in terms of node temperatures are set equal to residuals  $R_1$  to  $R_N$ . The object of the analyses is to make these residuals go to zero. To accomplish this a table is formed which indicates how large the changes are in residuals for a unit change in node temperature. By inspection, the largest residual is altered to go to zero by changing one of the temperatures. Changes in all of the residual terms are noted and residual terms adjusted. The next highest residual is examined and temperatures are changed to make it go to zero. This is repeated until all residual terms are zero or sufficiently close to zero to be considered negligible. The set of adjusted temperatures provides the desired temperature distribution through the material.

Node analysis for heat and mass flux into the catalyst required significant modification as undertaken in the ensuing investigation. Temperatures were found to be dependent upon the amount of reaction occurring in the nodes. Analysis assumed the outermost node exhibited pellet surface conditions. Surface rates were used to estimate rate equations. The sum of the reactions in all nodes was required to equal the total rate observed for the pellet. Node rates were limited to values less than that defined by diffusion rates and by the rate equation determined from the surface rate estimates.

1. Concentration distribution in pellet. With non-isothermal pellet data the achievement of steady state conditions required that mass flux into a node be zero. To simplify the computer program a spherical pellet was selected having four nodes, each node representing  $1/4$  of the pellet volume. Nodes in the spherical pellet were defined as the surfaces of a thin spheres located centrally in the node shells. It was assumed that the amount of reaction occurring in each shell could be represented at the node. For the purpose of calculation, the total rate of reaction in a pellet ( $r_t$ ) equals the sum of the rates in all four nodes. This means that transport of reactants and products is controlled by the concentration gradient for each. Thus for a reaction of  $A + B = R + S$ , the concentration drop between nodes may be determined from a set of equations describing flow between node  $N-1$  and  $N$ :

$$\begin{aligned}
 -RA(N) &= DE_A * AR(N)/DR(N) C_A(N) - C_{AS} \\
 -P*RA(N) &= DEP * AR(N)/DR(N) C_B(N) - C_{BS} \\
 H*RA(N) &= DER * AR(N)/DR(N) C_R(N) - C_{RS} \\
 Q*PA(N) &= DES * AR(N)/DR(N) C_S(N) - C_{SS}
 \end{aligned}
 \tag{36}$$

Here, the diffusion rate of each component is related to diffusion of species A or  $RA(N)$  times a coefficient determined by the mass balance from the reaction. Since product mass exiting equals reactant mass entering the node, the requirement that mass flux in equals mass flux out is satisfied.

Diffusion rates are controlled by a requirement to feed the reaction at the inside node. Reaction rates therefore influence the variation in concentrations observed. The solution for the concentration curve requires the solving of the above equations for  $C_A(N)$ ,  $C_B(N)$ ,  $C_R(N)$ , and  $C_S(N)$  at each node  $N$ . Main stream concentrations are assumed known. The  $N$  in bracket refers to the node number and is written in this discussion in Matrix notation similar to the Fortran IV designation.

2. Temperature distribution. Temperature through the pellet is related to the heat released at each node from the reaction occurring there. The heat flux rate is based upon the heat generated in the inner nodes which must flow out to satisfy pellet steady state temperature conditions.

$$\sum_{n=1}^4 R(N) * \Delta H = CK * AR(N)/DR(N) * (T_{N2} - T_{N1}) \quad (37)$$

Temperatures for each node are obtained by summing and adding these to the experimentally determined surface temperature.

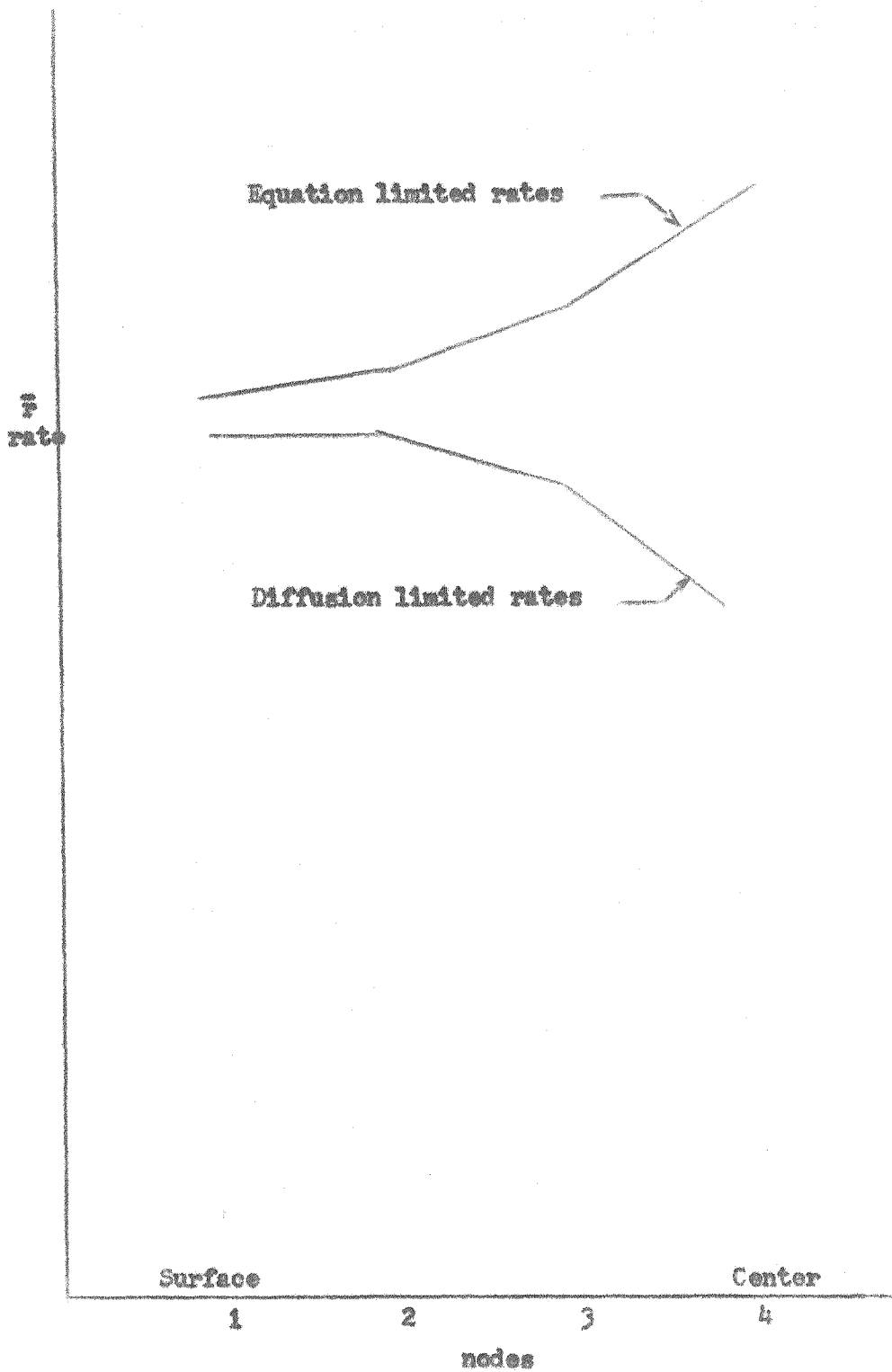
$$T_N = T_S + \sum \Delta T \quad (38)$$

3. Rate determination. For the initial least square approximation of the surface rates all of the reaction is assumed placed in the surface node. The program solves (via least square analysis) for the rate

equation and constants which fit the data for high and low catalyst surface temperatures. If rates are calculated for each node using the least square equation, the total quantity reacted would be about four times the total mass experimentally observed to react in the pellet. Subsequent approximations alter the equation to reduce the calculated rates. Next considering the other extreme, if all the reacting mass diffuses as far as possible into the pellet, we find that the total reacting mass diffuses into the first two or three nodes, but because of diffusion restriction, the total pellet reaction flow may not reach the last node. These two conditions are represented by the curves in Figure 1.

Rate determination is accomplished by first assuming an initial rate distribution through the pellet. In this analysis we assume that the pellet total rate is disseminated to the interior nodes to the maximum allowable by diffusion. Then by decreasing the equation estimated rates at each node, the reacting mass in the inner nodes are moved to the outer ones until all nodes rates summed equal the total pellet rate.

Chemical concentration variance is estimated based on the following assumption critical to the argument presented: The amount of diffusion (quantity of mass) traveling from one node to the next is controlled by the rate of reaction occurring in the innermost nodes. If we take the center (Innermost) node, the amount diffusing into the node is the amount being reacted there. An equal mass must leave the node -- in this case, the products of reaction. Product accumulation does not allow a steady state chemical composition in the node. In similar manner, the amount



**FIGURE 1**  
**RATE VS NODE**  
(Based upon Diffusion Limits Least Square Approximation - First Iteration)



of diffusion between second and third nodes can be estimated as equal to the quantity of reactant needed to feed the inner nodes three and four. The same holds true for diffusion between nodes one and two. For calculations of interior node concentrations, the surface node concentration must be known. Internal rates and resultant concentration gradients provide the driving force for flow of reactants into the inner nodes.

These concentrations and temperatures are subsequently used in the rate equation to calculate node rates. Estimates of node one rate (surface rate) are used to determine the Hinshelwood rate equation. Employing equation calculated interior node rates, a difference determined node one is estimated by subtracting the node two, three and four rates from the total pellet rate. If this node one rate is smaller than the rate used to define the equation, the equation rates are decreased by taking incrementally smaller surface rate estimates. To achieve this, a percentage cut of the last surface or node one estimate is used. This is done by using a multiplier term call ZD. The term ZD is decreased and then used to multiply all pellet last estimated node one rates.

$$ZD = 0.8 * ZD$$

$$r(1) = ZD * (\text{last node one estimate}) \quad (39)$$

A least square approximation from the decreased pellet node one rates is calculated. Next, all rates used to define the Hinshelwood equation are compared with the difference determined rates. This process is continued until the surface node for pellets provides a ZD \* (last node one estimate) product incrementally less than the difference determined node one rate yielding a rate versus node curve as shown in Figure 2.

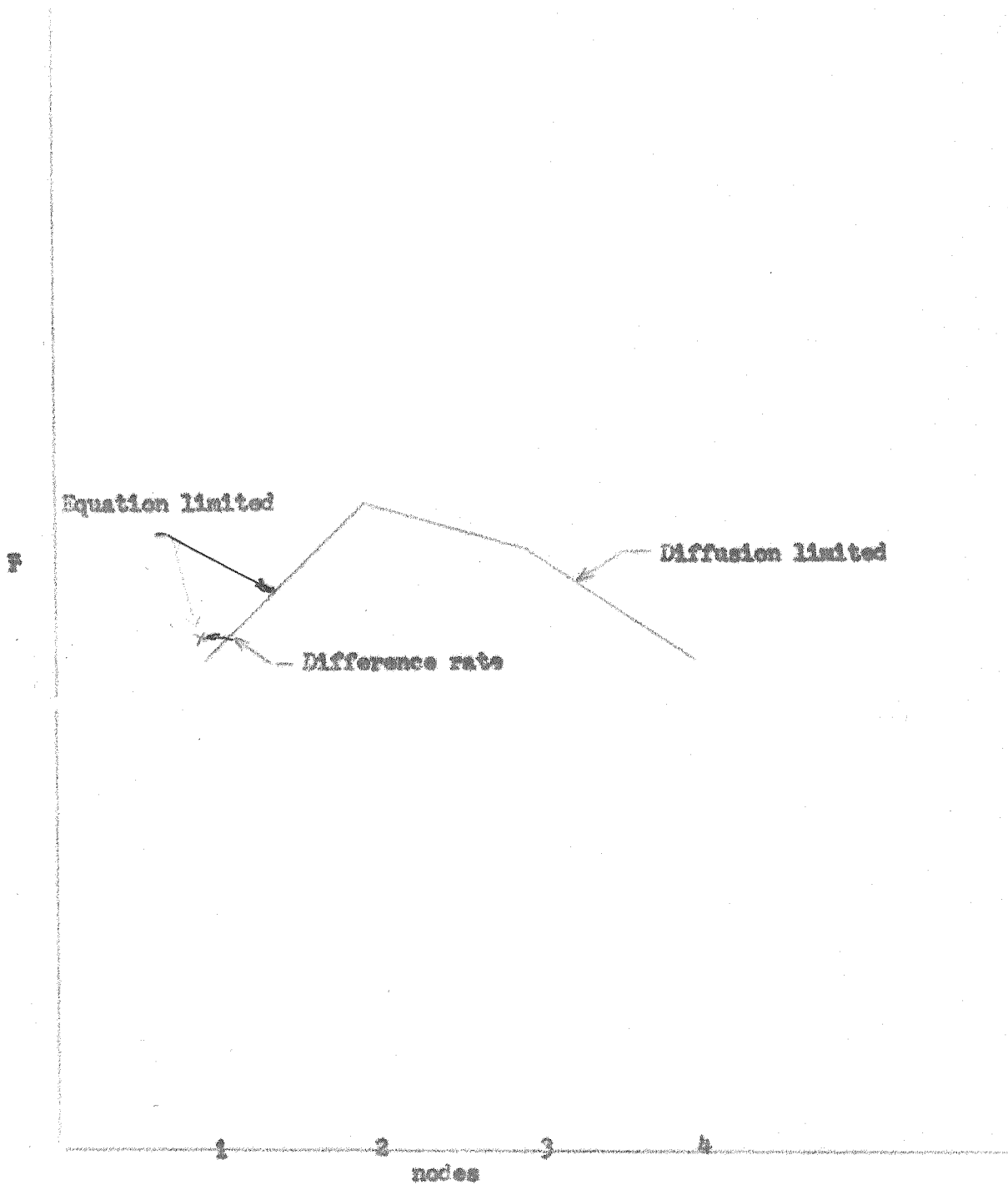


FIGURE 2  
RATE VS NODE  
(ZD \* last node estimate)

Up to this point, we considered single pellet analyses. The least square approximation rate curve is defined from many pellets. As indicated earlier, the least square equation defined from all pellets is modified until node one equation rates  $r(1)$  for all pellets are incrementally smaller than the difference determined node one rates. This means that one pellet sets the low value of rates and of  $ZD$ . The other pellet node one rates determined via the difference approach will tend to be high compared to their final value. If the difference between the least square approximation calculated rates ( $R_{ICALC}$ ) and the difference determined node one rates is small, the equation is accepted. When the difference as indicated by the coefficient of variation between node one rates calculated from the least squares approximation and difference determined node one rates deviates so as to reject the equation, the last difference determined node one rates are used for the next least square approximation. Thus, the shape of the curve is altered to reflect the high or low node one rates resulting from the previous pellet calculations. Each iteration should bring the least square approximated curve closer to the node one difference estimates as indicated in Figure 3.

3

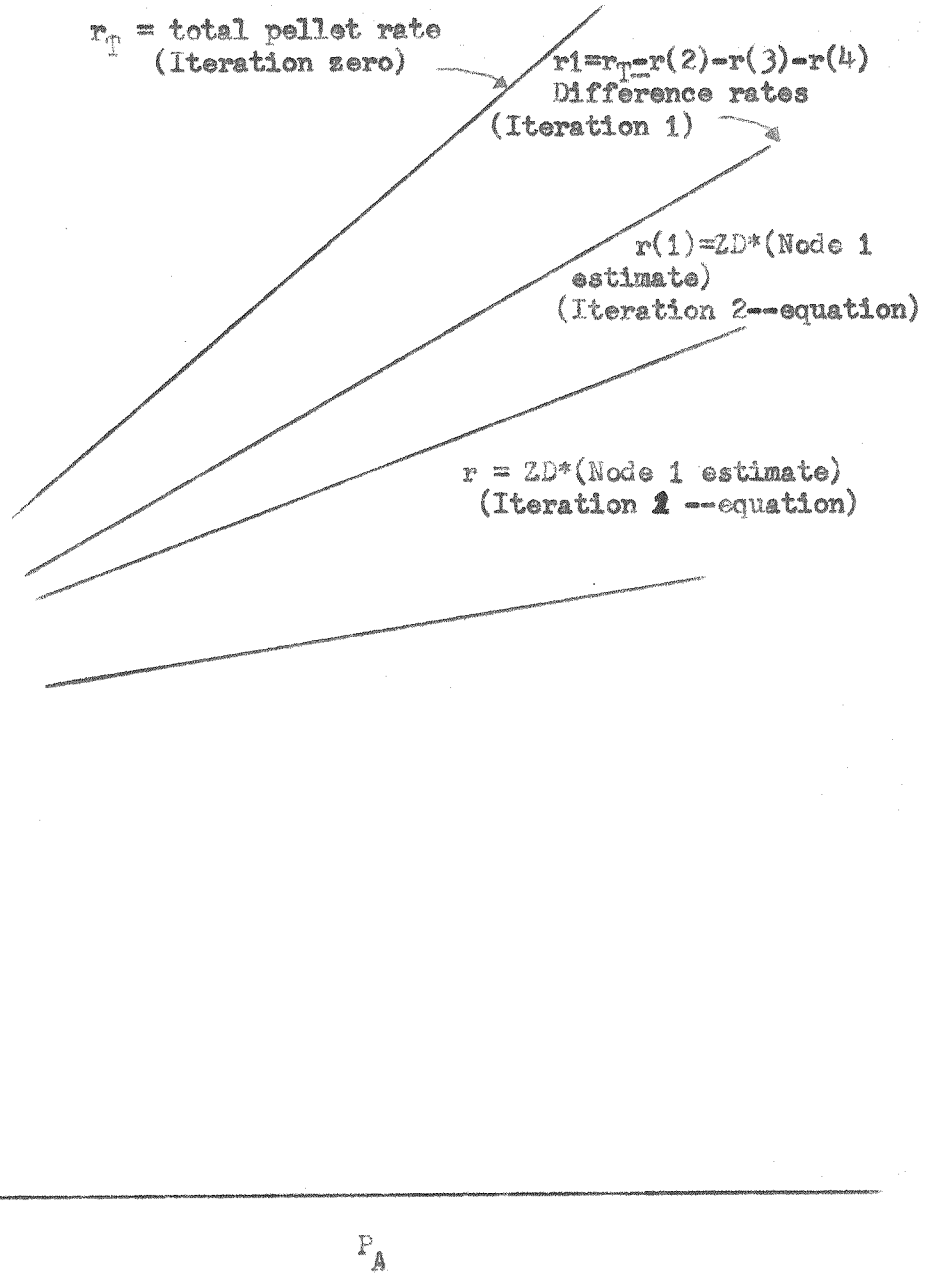


FIGURE 3  
SUCCESSIVE NODE 1  
VERSUS PARTIAL PRESSURE A ITERATIONS

### E. Node Program Description

It was concluded from the analysis that a Node method for determining Hinshelwood equations from catalyst data was feasible. In view of the extensive number of calculations needed to converge to a representative Hinshelwood equation for the surface rates, a computer program appeared to be the only reasonable means of attaining the solution. A computer program was thus assembled which was composed of three major sections or loops designed to perform the following computation:

1. Least square node one approximation.
2. Diffusion, temperature and node one rate determination.
3. Comparison of difference determined node one rates with the least square approximation node one rates.

These loops are shown in the computer control diagram presented in Figure 4. The diagram indicates the controls statements but only calls out the analysis to be performed in each part. The three major loops are initiated from an if statement indicated by a diamond on page 23A. The diamonds (IN:2) are in the diagram lines containing indicators  $I = 1$  and  $I = 2$ .

The indicators (I) are used to reference the storage matrices B and C. Storage matrices are defined as matrices in which experimental data has been placed. Prior to the three loop split the matrix values of B or C are transferred to working matrix A. Then, after performing computations in the first loop, the indicator I designates which matrix (B or C) the computed values are to be stored. We will consider operations in each loop in the following discussion. Input and output is discussed in the APPENDIX. A program printout is also shown in the APPENDIX.

FIGURE 4  
 COMPUTER CONTROL DIAGRAM (ONLY)  
 (Part A)

RATE MECHANISMS MQ, MW, MU, MY, MP, TN, VO

DATA MATRIX B, C

DIFFUSIVITIES DEA, DEB, DEC, DES

CONSTANTS BP, CP, HR, KF

MASS BALANCE F, H, Q

CONSTANTS UZ, CK, GC

ITERATIONS FN, FN

A

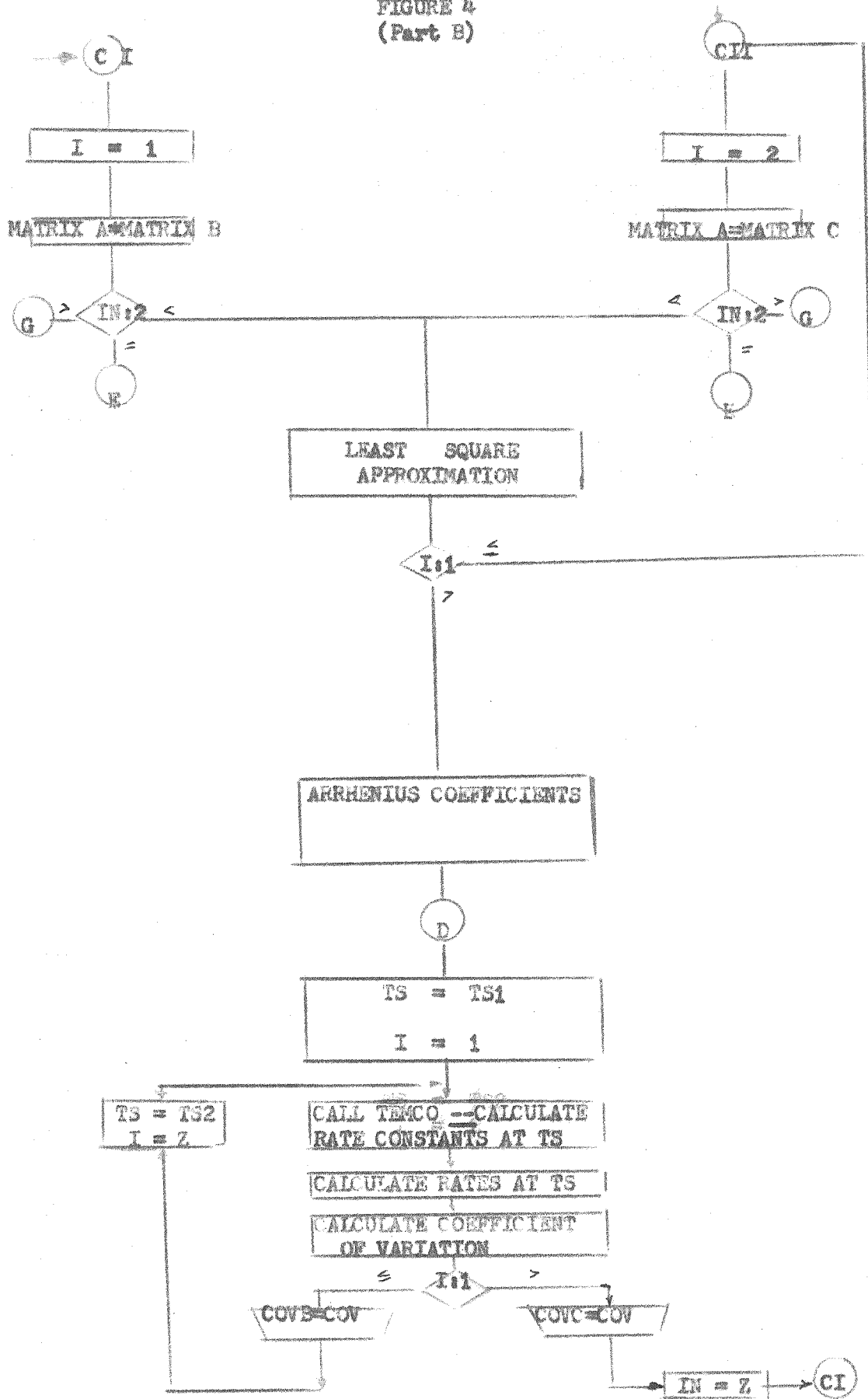
|     |            |
|-----|------------|
| KK  | = 1        |
| LP  | = 1        |
| N   | = TN(KK)   |
| LC  | = MQ(KK)   |
| LD  | = MW(KK)   |
| LP  | = MU(KK)   |
| LG  | = MY(KK)   |
| LH  | = (MP(KK)) |
| VOK | = VO(KK)   |
| TIM | = 0        |
| TIN | = 0        |

B

|                |                  |
|----------------|------------------|
| <del>TIN</del> | <del>= 1.0</del> |
| 2D             | = 1.0            |
| IZ             | = 1.0            |

C I

FIGURE 4  
(Part B)



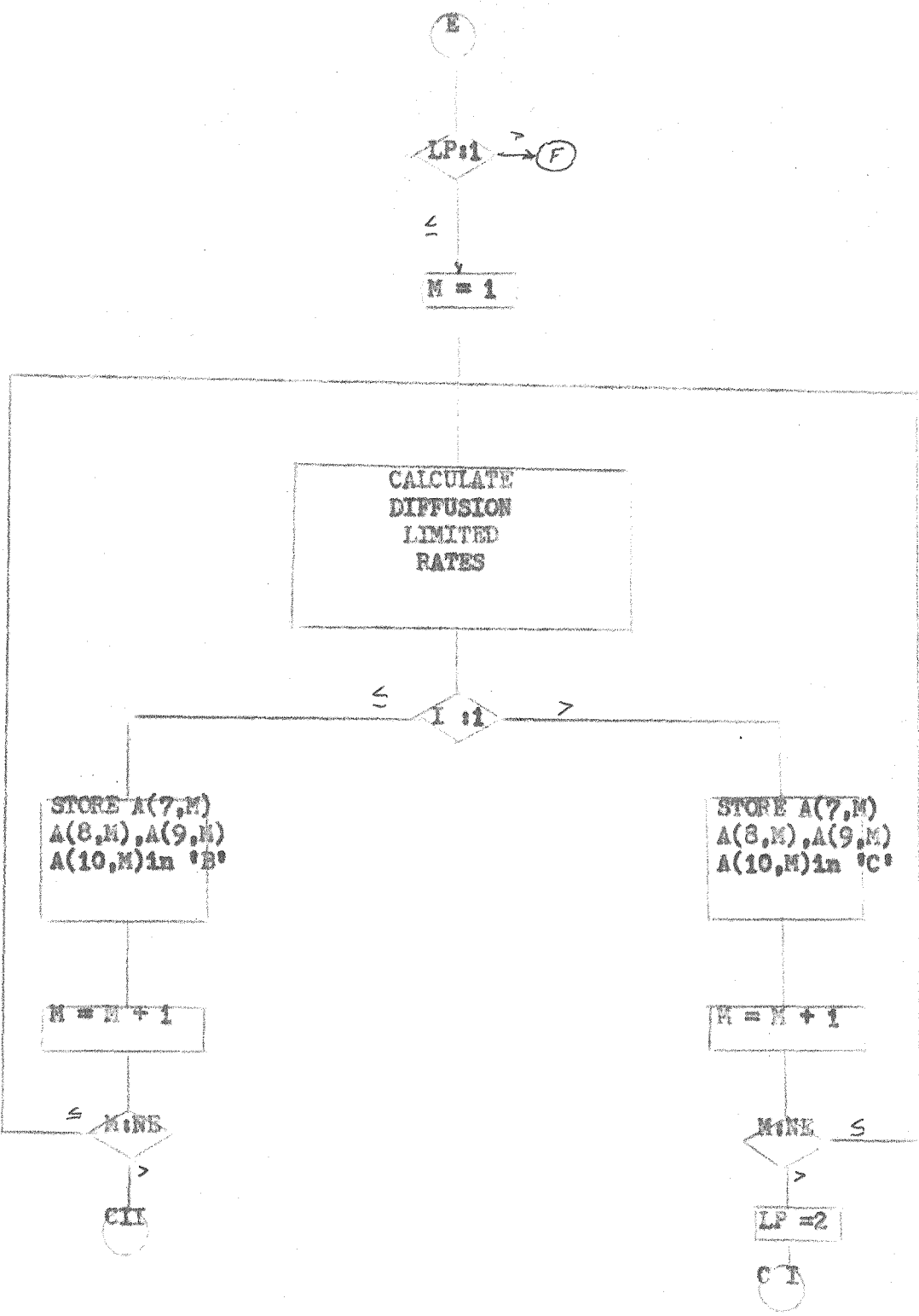


FIGURE 3  
(Part C)





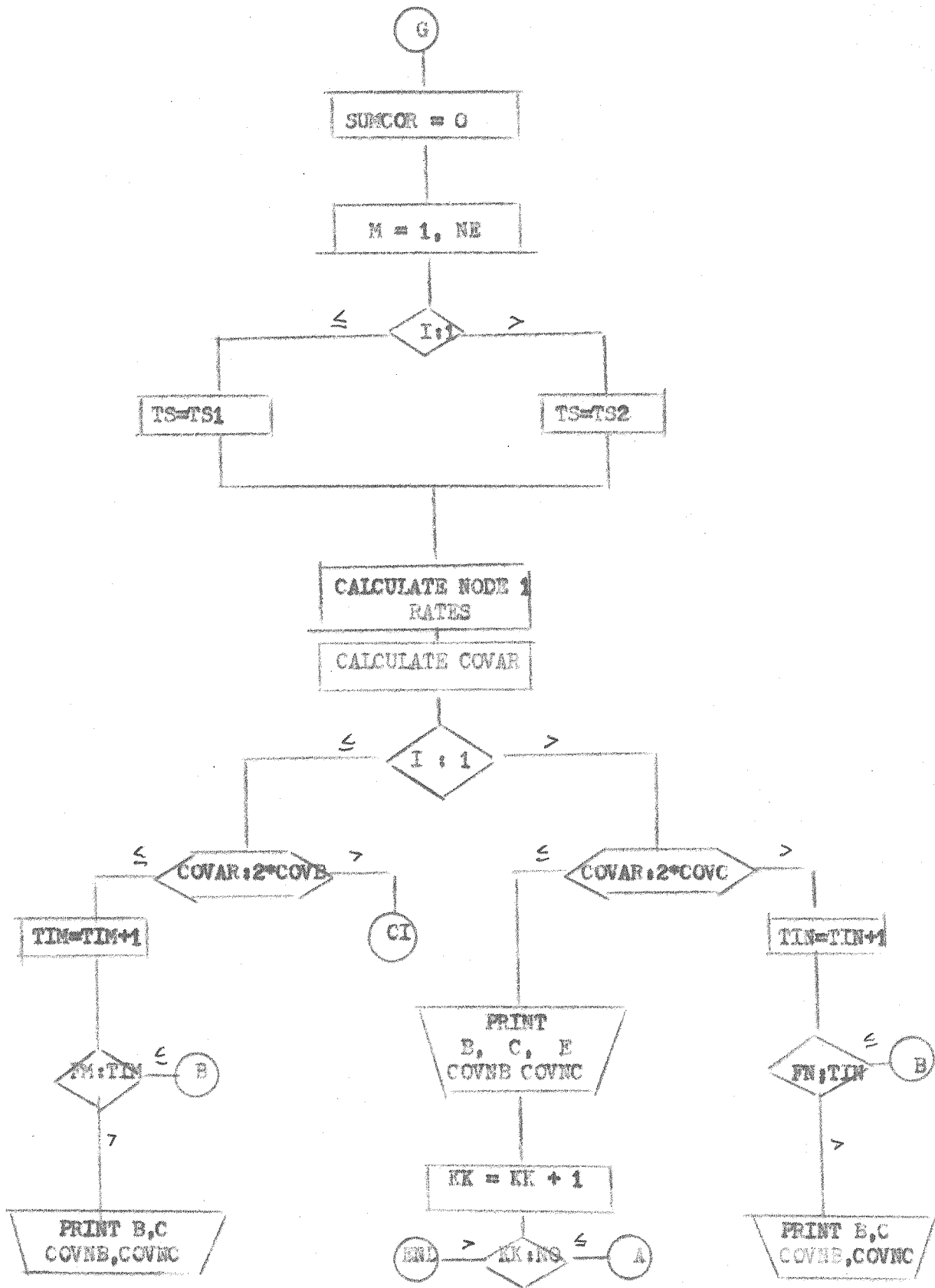


FIGURE 3  
(Part E)

1. Least square approximation loop (IN = 1). In loop 1 and node 1, rates and concentrations are used for defining the Hinshelwood rate equation. Node one rate estimates are initially specified in the input data. The Hinshelwood rate form is preselected by the programmer and called out in the input to the computer. Using the preselected rate forms, the computer performs a linear least square analysis of the surface rates evaluating the equation for the rate equation constants. These constants are used to calculate the Arrhenius constants. The last operation in the loop determine the closeness of fit of the equation derived rates to the previously determined node one rates. Closeness of fit of the difference determined node one rates and the Hinshelwood equation calculated rates is indicated by a coefficient of variation.

a. Hinshelwood rate equation. The calculations performed in loop one are as follows: The rate equation is assembled by calling for terms from several function subroutines. Rate forms are designated from addresses included in the program input. Refer to the Appendix for a more detailed description. The generalized rate form is defined by the equation:

$$r = \frac{\text{Kinetic term} * \text{potential term}}{(\text{adsorption Term})^N}$$

Table I through IV provides a list of terms in Kinetic, potential and individual adsorption terms encompassing those included in the subroutines. The equation is rewritten in terms of reactant and product concentrations as follows:

$$K_1 + K_2 * P_A + K_3 * P_B + K_4 * P_R + K_5 * P_S = \frac{(FOT)}{r} \quad 1/N \quad (40)$$

Table I Reaction Rate Mechanisms  
(Tables are from Ref. 9)

Part A

DRIVING POTENTIAL TERMS

| Reaction                                 | $A \rightleftharpoons R$ | $A \rightleftharpoons R+S$        | $A+B \rightleftharpoons R$ | $A+B \rightleftharpoons R+S$          |
|--|--------------------------|-----------------------------------|----------------------------|---------------------------------------|
| Adsorption of A controlling              | $a_A - \frac{a_R}{K}$    | $a_A - \frac{a_R a_S}{K}$         | $a_A - \frac{a_R}{K a_B}$  | $a_A - \frac{a_R a_S}{K a_B}$         |
| Adsorption of B controlling              | 0                        | 0                                 | $a_B - \frac{a_R}{K a_A}$  | $a_B - \frac{a_R a_S}{K a_A}$         |
| Desorption of R controlling              | $a_A - \frac{a_R}{K}$    | $\frac{a_A}{a_S} - \frac{a_R}{K}$ | $a_A a_B - \frac{a_R}{K}$  | $\frac{a_A a_B}{a_S} - \frac{a_R}{K}$ |
| Surface reaction controlling             | $a_A - \frac{a_R}{K}$    | $a_A - \frac{a_R a_S}{K}$         | $a_A a_B - \frac{a_R}{K}$  | $a_A a_B - \frac{a_R a_S}{K}$         |
| Impact of A controlling (A not adsorbed) | 0                        | 0                                 | $a_A a_B - \frac{a_R}{K}$  | $a_A a_B - \frac{a_R a_S}{K}$         |
| Homogeneous reaction controlling         | $a_A - \frac{a_R}{K}$    | $a_A - \frac{a_R a_S}{K}$         | $a_A a_B - \frac{a_R}{K}$  | $a_A a_B - \frac{a_R a_S}{K}$         |

Part B

REPLACEMENTS IN THE GENERAL ADSORPTION TERMS.

$$\left[ 1 + K_{A A_A} + K_{B B_B} + K_{R R_R} + K_{S S_S} + K_{I I_I} \right]^n$$

| Reaction   | $A \rightleftharpoons R$   | $A \rightleftharpoons R+S$     | $A+B \rightleftharpoons R$     | $A+B \rightleftharpoons R+S$       |
|--|----------------------------|--------------------------------|--------------------------------|------------------------------------|
| Where adsorption of A is rate controlling<br>replace $K_{A A_A}$ by                            | $\frac{K_A a_R}{K}$        | $\frac{K_A a_R a_S}{K}$        | $\frac{K_A a_R}{K a_B}$        | $\frac{K_A a_R a_S}{K a_B}$        |
| Where adsorption of B is rate controlling<br>replace $K_{B B_B}$ by                            | 0                          | 0                              | $\frac{K_B a_R}{K a_A}$        | $\frac{K_B a_R a_S}{K a_A}$        |
| Where desorption of R is rate controlling<br>replace $K_{R R_R}$ by                            | $K K_{R A_A}$              | $K K_{R A_A} \frac{K_A}{a_S}$  | $K K_{R A_A} a_B$              | $K K_{R A_A} a_B a_S$              |
| Where adsorption of A is rate controlling with dissociation of A<br>replace $K_{A A_A}$ by     | $\sqrt{\frac{K_A a_R}{K}}$ | $\sqrt{\frac{K_A a_R a_S}{K}}$ | $\sqrt{\frac{K_A a_R}{K a_B}}$ | $\sqrt{\frac{K_A a_R a_S}{K a_B}}$ |
| Where equilibrium adsorption of A takes place with dissociation of A<br>replace $K_{A A_A}$ by | $\sqrt{K_A a_A}$           | $\sqrt{K_A a_A}$               | $\sqrt{K_A a_A}$               | $\sqrt{K_A a_A}$                   |
| and similarly for other components adsorbed with dissociation.                                 |                            |                                |                                |                                    |
| Where A is not adsorbed<br>replace $K_{A A_A}$ by  | 0                          | 0                              | 0                              | 0                                  |
| and similarly for other components which are not adsorbed.                                     |                            |                                |                                |                                    |

Table I Reaction Rate Mechanisms  
(Continued)  
(Tables are from Ref. 9)

Part C

KINETIC TERMS.

Multiply each of the terms below by EL except for the homogeneous reaction.

|   |                   |
|---|-------------------|
| Adsorption of A controlling                   | $k_A$             |
| Adsorption of B controlling                   | $k_B$             |
| Desorption of R controlling                   | $k_R K$           |
| Adsorption of A controlling with dissociation | $\frac{s}{2} k_A$ |
| Impact of A controlling                       | $k_A K_B$         |
| Homogeneous reaction controlling              | $k$               |

Surface Reaction Controlling

|                               | $A \rightleftharpoons R$ | $A \rightleftharpoons R+S$ | $A+B \rightleftharpoons R$ | $A+B \rightleftharpoons R+S$ |
|-------------------------------|--------------------------|----------------------------|----------------------------|------------------------------|
| Without dissociation          | $k_s K_A$                | $k_s s K_A$                | $k_s s K_A K_B$            | $k_s s K_A K_B$              |
| With dissociation of A        | $k_s s K_A$              | $k_s s K_A$                | $k_s s (s-1) K_A K_B$      | $k_s s (s-1) K_A K_B$        |
| B not adsorbed                | $k_s K_A$                | $k_s s K_A$                | $k_s K_A$                  | $k_s s K_A$                  |
| B not adsorbed, A dissociated | $k_s s K_A$              | $k_s s K_A$                | $k_s s K_A$                | $k_s s K_A$                  |

Part D

EXPONENTS OF ADSORPTION TERMS

|   |         |
|---|---------|
| Adsorption of A controlling without dissociation              | $n = 1$ |
| Desorption of A controlling                                   | $n = 1$ |
| Adsorption of A controlling with dissociation                 | $n = 2$ |
| Impact of A without dissociation $A + B \rightleftharpoons R$ | $n = 1$ |
| Impact of A without dissociation $A+B \rightleftharpoons R+S$ | $n = 2$ |
| Homogeneous reaction  | $n = 0$ |

Surface Reaction Controlling

|                                       | $A \rightleftharpoons R$ | $A \rightleftharpoons R+S$ | $A+B \rightleftharpoons R$ | $A+B \rightleftharpoons R+S$ |
|---------------------------------------|--------------------------|----------------------------|----------------------------|------------------------------|
| No dissociation of A                  | 1                        | 2                          | 2                          | 2                            |
| Dissociation of A                     | 2                        | 2                          | 3                          | 3                            |
| Dissociation of A (B not adsorbed)    | 2                        | 2                          | 2                          | 2                            |
| No dissociation of A (B not adsorbed) | 1                        | 2                          | 1                          | 2                            |

This equation form is used for linear fitting of the node one rate data. The linear least square analysis is performed as described by Hougen and Watson (8). Values for the terms  $K_1$ ,  $K_2$ ,  $K_3$ , and  $K_4$  and  $K_5$  are stored in a matrix E in preparation for the next step that of computation of the Arrhenius constants.

b. Arrhenius constant determination. After the rate constants in loop one are calculated for the matrix B and matrix C data at two surface temperatures, the temperature dependence of the constants is represented by the Arrhenius exponential function:

$$K = K_0 \exp(-A/RT) \quad (41)$$

Where  $K_0$  and A are constants to be determined, R is the universal gas constant and T is the temperature of the reaction. The Arrhenius constants are determined by taking the log form of the above equation. Substituting into two simultaneous equations the  $K_{1B}$  and  $K_{1C}$  constants from matrix E, A and  $K_0$  are then defined by the equations below.

$$A = R (TS_1 - TS_2 / TS_1 * TS_2) \log (K_{1B} / K_{1C})$$

$$K_0 = K_{1B} \exp (A/R * TS_1)$$

The Arrhenius constants in the computer program are defined as AK for  $K_0$  and DB for A.

c. Coefficient of variation. The coefficient of variation indicates how far apart the node one rates are from the equation determined rates. A coefficient of variation is determined for each matrix (B and C) in the following manner. We set the temperature (T) for the Arrhenius constant equal to the surface temperature and compute values for the Hinshelwood

constants using the Arrhenius equation. Rates are calculated for each pellet based upon these constants and the surface concentrations of the species.

$$RC = \frac{K}{(K_1 + K_2 * P_A + K_3 * P_B)^N} * POT \tag{43}$$

These calculated rates are then compared with the rates R(1) determined from either the initial estimate supplied by the programmer in the input or from the difference determined node one rates which are calculated in loop two and stored in terms B(10,M) or C(10,M).

$$R(1) = (\text{total rate}) * (\text{multiplier defined in the program})$$

The multiplier is the product of the node one rate fraction from matrix terms B(10,M) or C(10,M) and the value of ZD which is set equal to 1 for the first iteration but is decreased in loop two during subsequent iterations. The term M corresponds to the pellet assigned number in the matrix.

The coefficient of variation is determined from the rates by solving the following equation:

$$COV(B \text{ or } C) = \frac{\sqrt{((RC) - R(1))^2}}{N - 1} \tag{44}$$

When coefficients of variation have been computed for data in matrix B and C, the computer sets IN equal to 2 sending the program to loop two indicated as Location E in the diagram.

2. Diffusion, temperature, and node one rate determination (IN = 2).

The second loop location E, performs several key operations. The calculations performed in this loop determine diffusion rate limits, node

temperature, node concentrations, and node rates. The first calculation for diffusion limits is performed when indicator LP in loop two equals 1. The calculations employ average effective diffusivities at temperatures observed for the nodes. Temperature dependent diffusivities may be introduced into the program but average values were selected here to simplify calculation. After determining the diffusion limits for all data points, LP is set equal to 2 and further analyses bypass this section.

The second section of loop two calculates temperatures at each node. An initial rate estimate for the nodes is that the pellet reacting mass is diffused into the pellet as far as possible. In some cases this results in all of the reaction occurring in node four (all reacting mass diffusing into center node). The method of analysis used starts with high estimates of interior node rates and decreases the rates in each of the innermost nodes two, three and four by decreasing the linear least square approximation rates. The outermost node (node one) rate referred to as the difference determined rate is the rate determined from the total pellet rate less the rates from nodes two, three and four. When the difference determined node one rates become incrementally larger than the estimated surface rate we know the sum of the node rates must be slightly less than the total observed pellet reaction rate. This condition exists because the difference determined rate is larger than the surface rate estimate which was used to define the rate equation and calculate node two, three and four rates. These node one rates are forwarded to loop three for a final comparison of the rates determined from the equation versus those from the difference methods.



a. Diffusion limited rates. The calculations performed in loop two are as follows: In section one of loop two calculations of the mass flux between the nodes is determined. Several assumptions are made. The maximum flow of reactant into the pellet is assumed not to exceed the total reaction taking place in the pellet. Diffusion of each reactant and product is assumed related by the chemical reaction mass balance to one another. Thus, the reaction concentration diminishes proportionately to increases in product concentration. For a given pressure and temperature, the total number of moles/unit volume for a gas is known. The sum of the molar concentrations of the reactants and products in the node, moles per unit volume, must be equal to the total molar concentration moles/unit volume. Concentrations are subsequently calculated for each node with the exception that node one is assumed to have the same concentration as that of the main stream.

Starting with total rate of reaction of A in the pellet to be that diffusing to node two, the concentrations at node two is determined from the following equations. Terms AR and DR are the mean transfer area and distance between nodes respectively and RA is the diffusion rate of specie A. Terms  $C_{AS}$  to  $C_{SS}$  are surface concentrations.

$$\begin{aligned}
 C_A &= - RA * DR(2)/(DEA * AR(2)) + C_{AS} \\
 C_B &= - F * RA * DR(2)/(DEB * AR(2)) + C_{BS} \\
 C_R &= + H * RA * DR(2)/(DER * AR(2)) + C_{RS} \\
 C_S &= + Q * RA * DR(2)/(DES * AR(2)) + C_{SS}
 \end{aligned}
 \tag{45}$$

This process is repeated for node three assuming the values of  $C_A$

through  $C_S$  determined for node two are the new values of  $C_{AS}$  to  $C_{SS}$ . After calculating each set of concentrations, the concentrations are summed and compared with the total number of moles which a node (1/4 pellet volume) will hold. The total node quantity is bracketed by limits  $FD$  and  $FR$  placed in the program input.

$$\begin{aligned} (C_A + C_B + C_R = C_S) & : FD \\ (C_A + C_B + C_R + C_S) & : FR \end{aligned} \quad (46)$$

If the sum falls outside these limits, the value of  $RA$  is decreased.

$$RA = 0.95 * RA \quad (47)$$

It is known that for  $RA$  equal to zero the concentration must be that of the surface concentrations  $C_{AS} + C_{AB}$  etc. Thus it is expected as  $RA$  goes to zero that some value of  $RA$  will provide a total concentration that falls within the defined limits  $FD$  and  $FR$ .

b. Temperature determination in nodes. Returning to section two of loop two, the temperatures are determined on the basis that heat generated by the reaction must flow out of the pellet for thermal equilibrium. The  $\Delta T$  can be determined if an effective conductivity is used in the following equation:

$$Q = F(N) * HR = (CK * AR(N) * \Delta T) / DR(N) \quad (48)$$

The temperature rise from node to node is determined and added to the surface temperature to determine the node temperature. For each iteration node temperatures are recomputed.

$$T = TS + \sum \Delta T \quad (49)$$

c. Difference determination of node 1 rates.  $R(N)$  In the determination of representative node one rates a reduced rate term  $R(N)$  is compared with diffusion limit rate  $RA(N)$  and the calculated rate  $R1\text{ CALC}$ .  $R1\text{ CALC}$  is determined from the least square approximation using node temperatures and concentrations estimated. If  $R(N)$  is larger than either of these rates, an increment of rate is removed from the node reducing  $R(N)$ . The increment of reaction is then placed in the next outermost node.

Since initial node rates are determined from difference of diffusion into and out of the nodes, all of the reacting mass  $RA(N)$  is allowed to diffuse to the innermost nodes, therefore if anything is changed, it is the removing of some of the reaction from the inner nodes. The rates in each node one to four are compared with diffusion limited rate and with the calculated rates from the Hinshelwood equation employing Arrhenius constants. If there is more reaction in the node than allowed by these limits,  $R(N)$  is decreased.

$$R(N) = 0.95 * R(N) \quad (50)$$

When  $R(N)$  falls within these limits (Least square approximation and diffusion limits) the rate is considered representative of that node rate. Then, using a node one difference rate (total rate less inner node rates) a comparison is made between the node one rate and one defined by the product of  $ZD$  and the initial node 1 rate estimate. To obtain the initial node one estimate, the product  $A(10,M) * A(5,M)$  is determined where  $A(10,M)$  is the node rate fraction inputted or calculated and  $A(5,M)$  is the total rate. If from the comparison we find the difference rate is the lesser, the value of  $ZD$  is decreased.

$$ZD = 0.8 * ZD \quad (51)$$

The new value of ZD is sent back to loop one and multiplies all node one rates stored in matrix B and C. The ZD modified rates are used to obtain another least square approximation; a new Arrhenius constant, a new coefficient of variation and the program returns to loop two where the same rate adjustment process is continued. This process is repeated until the difference determined rates for the pellets are greater than the respective values of the product ZD and the initial node one rate estimate. When the node one rates are defined, they are stored in matrix B and C as B(10,M) and C(10,M) and are forwarded to loop three.

3. Loop three acceptance or rejection of least square linear approximation. The last loop (G) determines a second coefficient of variation. This time it provides a measure of deviation between the difference determined node one rates and the least square equation node one rates. The new coefficient of variation COVAR is then compared with the previous coefficient of variation COV. In the program as it presently stands, if COVAR is less than twice COV, the equation is accepted and constants printed out.

The calculations performed in this section repeat those performed in section one, part C, with the exception that the initial and final coefficients of variation (COV and COVAR) are compared.

### F. Hydrogen Oxygen Catalysis - Sample Problem

A sample case, Hydrogen - Oxygen over platinum catalyst was used to determine the types of problems which might be encountered in the proposed computer analysis. Data was reviewed from two papers. The papers described experimental studies in which the first paper investigated catalyst particles and pellets subjected to mixed streams of Hydrogen and Oxygen gas simulating a stirred tank reactor, and the second paper studied catalysis of Hydrogen/Oxygen in a small tubular flow integral reactor. In the former paper by Maymo and Smith (6) the low oxygen concentration range (0-4 mole %) was examined and it was concluded that rates were nearly first order with respect to oxygen partial pressure:

$$R = 0.655 \exp\left(\frac{-5230}{RT}\right) P_{O_2}^{0.804} \quad (52)$$

Leder and Butt (2) studied the low hydrogen end of the gas mixture range and concluded that a Hinshelwood equation represented the data. They concluded that surface adsorbed oxygen reacting with hydrogen in the gas phase controlled rates thus providing correlation with the following rate equation:

$$R = \frac{K P_{O_2} P_{H_2}^2}{1 + K_O P_{O_2} + K_W P_W} \quad (53)$$

Maymo and Smith also noted that reactions at high oxygen/low hydrogen mixture ratios were second order with respect to hydrogen concentration. The problem posed is: does the mechanism implied by the Hinshelwood equation submitted by Leder and Butt provide an acceptable rate form for the data at the opposite ends of the hydrogen/oxygen mixture range obtained by Maymo and Smith?

1. Test data. Data from (5) is summarized in Table II, part A. Rates were reported by Maymo and Smith in moles per gram - second but in this application, rates for entire pellets (average weight 2.0 grams) are listed because the total pellet rate was used in the analysis. The rates at oxygen partial pressure varying from 0.009 to 0.111 atmospheres ranged from  $19.2 \times 10^{-6} \frac{\text{moles}}{\text{pellet sec.}}$  to  $267 \times 10^{-6} \frac{\text{moles}}{\text{pellet sec.}}$ . The observed surface temperatures were between  $89^{\circ}\text{C}$  and  $180^{\circ}\text{C}$ . Other parameters reported and used in the computer analysis were the effective diffusion rate for oxygen of  $0.166 \text{ cm}^2/\text{sec}$ , the effective conductivity of the pellet  $6.4 \times 10^{-4} \text{ cal/cm(sec)} (^{\circ}\text{C})$  and the heat of reaction of  $115,000 \text{ cal/gm mole}$ . All other values used were selected or calculated. Diffusivities of hydrogen ( $4.37 \frac{\text{cm}^2}{\text{sec}}$ ) and water vapor ( $0.6 \text{ cm}^2/\text{sec}$ ) were estimated from the effective diffusivity equations employing bulk and Knudsen diffusion. Specific heat and equilibrium constant were obtained from the Handbook of Physics and Chemistry. The results of several computer runs performed with input data (Table II, Part B) are discussed in the following sections.

2. Computer results. Several computer runs were made to determine if the Hinshelwood equation proposed by Leder and Butt would fit the experimental rate data of Maymo and Smith. The forms used were as follows:

$$\begin{aligned} \text{(a) } r &= P_{O_2} / (K_1 + K_2 * P_{O_2}) \\ \text{(b) } r &= P_{O_2} * P_{H_2} / (K_1 + K_2 * P_{O_2}) \end{aligned} \quad (54)$$

In determining the equation constants the program employs the partial pressures of Hydrogen and Oxygen in the following equations:

$$K_1 + K_2 * P_{O_2} + K_3 * P_{H_2} = \frac{(P_{O_2} P_{H_2} - P_{H_2O}/K_E)}{r} \quad (55)$$

TABLE II  
PART A  
RATE DATA (6)

| Pellet<br>Number | Surface<br>Temperature<br><br>°C | Oxygen<br>Concentration<br><br>$\frac{\text{mole/cm}^3}{\text{atm}}$ | Hydrogen<br>Concentration<br><br>$\frac{\text{mole/cm}^3}{\text{atm}}$ | Pellet Rate<br>mole/pellet<br>sec<br>( $r \times 10^6$ ) |
|------------------|----------------------------------|--|--|--|
| 11-1             | 101                              | 0.029  | 0.971  | 57.8   |
| 11-2             | 101                              | 0.054  | 0.946  | 101.0  |
| 11-3             | 100                              | 0.0094   | 0.991  | 19.2   |
| 12-3             | 102                              | 0.060  | 0.940  | 106.0  |
| 24-1             | 206                              | 0.046  | 0.954  | 267.0  |
| 24-3             | 130                              | 0.046  | 0.954  | 110.0  |
| 24-1             | 117                              | 0.111  | 0.889  | 248  |
| 21               | 127                              | 0.027  | 0.923  | 81   |
| 21               | 181                              | 0.027  | 0.973  | 118  |

TABLE II  
PART B  
IN-PUT DATA (2)

| In-Put Description  | Computer Term              | Example Value  |
|---|----------------------------|--|
| 1. Number of rate mechanisms  | NO                         | 2  |
| 2. Rate mechanism (addresses)   | MQ, MU, MV, MY, MZ, TN, VO | 2, 11, 1, 2, 2, 1, 3   |
| 3. Number of Data Points  | MF, NF                     | 4, 2   |
| 4. Matrix B Data  | B(1, 1)<br>B(14, MF)       | .027, 0.973, 0, 0,<br>0.1E-04, 1, 1, 1, 1,<br>.025, 1.0, 1.0, 1.0, 1.0 |
| 5. Matrix C Data  | C(1, 1)<br>B(14, MF)       | Same   |
| 6. Diffusion Constants  | DEA, DEB, DER,<br>DES      | 0.166, 0.60, 1.0, 0  |
| 7. Constants: Pellet radius, Specific Heat of Gas, Heat of Reaction, Equilibrium Constant                             | RP, CP, HR, KE             | 0.93, 7.0, 115,000, 2,000  |
| 8. Constant: From Mass Balance<br>$A + F \cdot B \rightarrow H \cdot R + Q \cdot S$<br>$O_2 + 2H_2 \rightarrow 2H_2O$ | F, H, Q                    | 2, 2, 0  |
| 9. Surface Temperatures   | TS1, TS2                   | 373°K, 403°K   |
| 10. Constants: Number of Constants to be solved for, effective Thermal Conductivity of Pellet, Universal Gas Constant | U2, CK, GC                 | 2, $6.5 \times 10^{-4}$ , 1.98   |
| 11. Number of Iterations  | FM, FN                     | 3, 3   |



Solution involves determination of  $K_1$ ,  $K_2$ , and  $K_3$  for each mechanism investigated. The constant for water is indeterminable because of pallet surface water vapor pressure being negligible. To determine if the constant  $K_3$  is zero for the case of adsorbed oxygen reacting with hydrogen in the gas phase, it is necessary to solve for the three constants but if one of the constants is zero, the subroutine SOLV now in use (see Appendix) writes out the word EXTOL. The computer bypasses further calculation of that case. Thus the method of evaluating the constant is to run three rate forms. The first form with all constants  $K_1$ ,  $K_2$ , and  $K_3$ . The second rate form with  $K_1$  and  $K_2$  only setting  $K_3$  equal to zero, and the third rate form containing only  $K_1$  and  $K_3$  setting  $K_2$  equal to zero. It is noted that the simultaneous equation solution performed by subroutines MAT and SOLV when replaced by the existing computer library subroutines will print out zeros for these constants which are zero and accomplish this analysis in one run.

3. Discussion of Computer analysis performed. During this investigation, computer runs were performed on oxygen/hydrogen rate data. The analyses considered calculation of constants  $K_1$  and  $K_2$  assuming  $K_3$  zero. Equations examined were as follows:

$$(1) \quad r = \frac{P_{O_2}}{K_1 + K_2 * P_{O_2}}$$

and

$$(2) \quad r = \frac{P_{O_2} * P_{H_2}^2}{K_1 + K_2 * P_{O_2}}$$

(56)

Four data points were placed in matrix B all having surface temperatures of 373° K and two pellet data points placed in matrix C with surface temperatures of 403° K. An iteration limit of three was imposed to limit machine time. Initial runs indicated that convergence was occurring extremely slowly and results of node one rate comparison indicated wide deviation existed at the end of three iterations and so the number of pellet points were reduced to three in matrix B. The next run appeared to converge more rapidly than the previous one, but did not reach convergence within the three iterations allowed. Therefore, the number of points in matrix B was decreased to two and the iteration limit increased to five. Convergence to a fixed value appeared to have been achieved in this run. The coefficients of variation for the two mechanisms were close with the coefficient for mechanism two appearing slightly better as indicated in Table III. The rate equation defined for the second mechanism can be written as follows placing the values of  $K_1$  and  $K_2$  in Arrhenius constant form in the denominator:

$$r = \frac{P_{O_2} P_{H_2}^2}{0.0128 \exp \left( \frac{10800}{RT} \right) + (639T - 2,600,000) P_{O_2}} \quad (57)$$

The linear form of the equation for the temperature dependant constant is used if one or more constants determined from least square analysis are negative. The Hinshelwood constants printed out in program are tabulated in Table IV.

The rate data comparison between calculated node one and difference determined node one rate are summarized in Table V.

TABLE III  
COEFFICIENTS OF VARIATION

| <u>Mechanism</u>                                | <u>COVN B</u> | <u>COVN C</u> |
|---|---------------|---------------|
| $r = P_{O_2} / (K_1 + K_2 * P_{O_2})$           | 0.166 E-04    | 0.224 E-04    |
| $r = P_{O_2} P_{H_2}^2 / (K_1 + K_2 * P_{O_2})$ | 0.164 E-04    | 0.140 E-04    |

TABLE IV  
RATE CONSTANTS ( $H_2/O_2$ )

|          |             | Hinshelwood | Coefficients |
|----------|-------------|-------------|--------------|
|          | Temperature | $K_1$       | $K_2$        |
| Matrix B | 373° K      | 2230        | - 22000      |
| Matrix C | 403° K      | 765         | - 2840       |

TABLE V  
 COMPARISON OF RATE DATA  
 (Iteration Mechanism)

|        | $P_{O_2}$ | $P_{H_2}$ | <u>Node 1</u><br>Calc. | <u>Node 1</u><br>Difference | <u>Total</u><br>Pellet Rate |
|--------|-----------|-----------|------------------------|-----------------------------|-----------------------------|
| Matrix | .0283     | 0.972     | $16.6 \times 10^{-6}$  | $20.9 \times 10^{-6}$       | $57.8 \times 10^{-6}$       |
| B      | .0580     | 0.942     | $54.0 \times 10^{-6}$  | $68.0 \times 10^{-6}$       | $106 \times 10^{-6}$        |
| Matrix | .027      | 0.973     | $37.1 \times 10^{-6}$  | $49.5 \times 10^{-6}$       | $81 \times 10^{-6}$         |
| C      | 0.044     | 0.956     | $62.9 \times 10^{-6}$  | $78.6 \times 10^{-6}$       | $110 \times 10^{-6}$        |

The calculated rate varies from the difference determined rates in each case by a factor of 0.8 which is equal to the size of an iteration step used. Iteration steps were made large to reduce computer run time but for greater accuracy the iteration step needs to be decreased such that the product of  $\Delta D$  and the rate multiplier varies only a few percent instead of the 20% used in this case. A second conclusion drawn from the table is that a large portion of the total rate is estimated to be occurring in node one. Looking at the matrix print out we get a reading of the reacted fractions for each node in Table VI. From the node rate fractions shown in the table the amount of the reaction taking place in node one increases with pellet rate. In the ensuing discussion it is seen that this condition is a result of the temperature sensitivity of the Hinshelwood rate constants which may or may not result from a recognizable physical phenomenon.

4. Discussion of analysis. From the analysis we are interested in whether the Hinshelwood rate form fits the data and whether the node one rates are of similar magnitude to the intrinsic rates obtained for particles. The first question is undoubtedly debatable because very little data was used, and there is some question of how representative the data was. However, in reviewing the runs performed, there appeared to be a consistent pattern in the way the Hinshelwood constants ( $K_1$  and  $K_2$ ) in the equation:

$$K_1 + K_2 * P_{O_2} = \frac{POT}{r} \quad (58)$$

behaved with temperature. In all cases  $K_1$  decreased slightly (see Table IV) with temperature increase while  $K_2$  underwent a major increase.

TABLE VI  
NODE RATE FRACTIONS

| Point  | MATRIX B |       | MATRIX C |        |
|--------|----------|-------|----------|--------|
|        | 1        | 2     | 1        | 2      |
| Node 1 | 0.36     | 0.642 | 0.609    | 0.714  |
| Node 2 | 0.352    | 0.207 | 0.199    | 0.146  |
| Node 3 | 0.201    | 0.107 | 0.123    | 0.0963 |
| Node 4 | 0.0859   | 0.044 | 0.0687   | 0.044  |

The rise in  $K_2$  was so pronounced that rates dropped off with distance into the interior of the pellets. Physically it does not appear reasonable that such a change in adsorption equilibrium constant would take place, and for this reason the mechanism proposed by Lader and Butt at low hydrogen high oxygen concentration does not seem applicable to the Mayo and Smith data.

In regard to calculated rates equations several results are noted. The first iteration in the case number 2 provided an equation indicated as follows:

$$r = \frac{P_{O_2} P_{H_2}^2}{0.411 \exp\left(\frac{6180}{RT}\right) + 1.66 \times 10^{11} \exp\left(\frac{-13100}{RT}\right) P_{O_2}} \quad (59)$$

If we assume negligible value for  $P_{O_2}$  we can rewrite the equation as follows:

$$r = 2.5 \exp\left(\frac{-6180}{RT}\right) P_{O_2} P_{H_2}^2 \quad (60)$$

This activation energy (6180) does not differ greatly from that reported by Mayo and Smith.

$$r = 0.655 \exp\left(\frac{-5230}{RT}\right) * P_{O_2} \quad (61)$$

However, after five iterations, the equation was altered to the following form:

$$r = \frac{P_{O_2} P_{H_2}^2}{.0128 \exp\left(\frac{10800}{RT}\right) + (639T - 2,600,000) P_{O_2}} \quad (62)$$

or in this case, assuming negligible  $P_{O_2}$  the equation becomes the following:

$$r = 80 \exp\left(\frac{-10800}{RT}\right) P_{O_2} P_{H_2}^2 \quad (63)$$

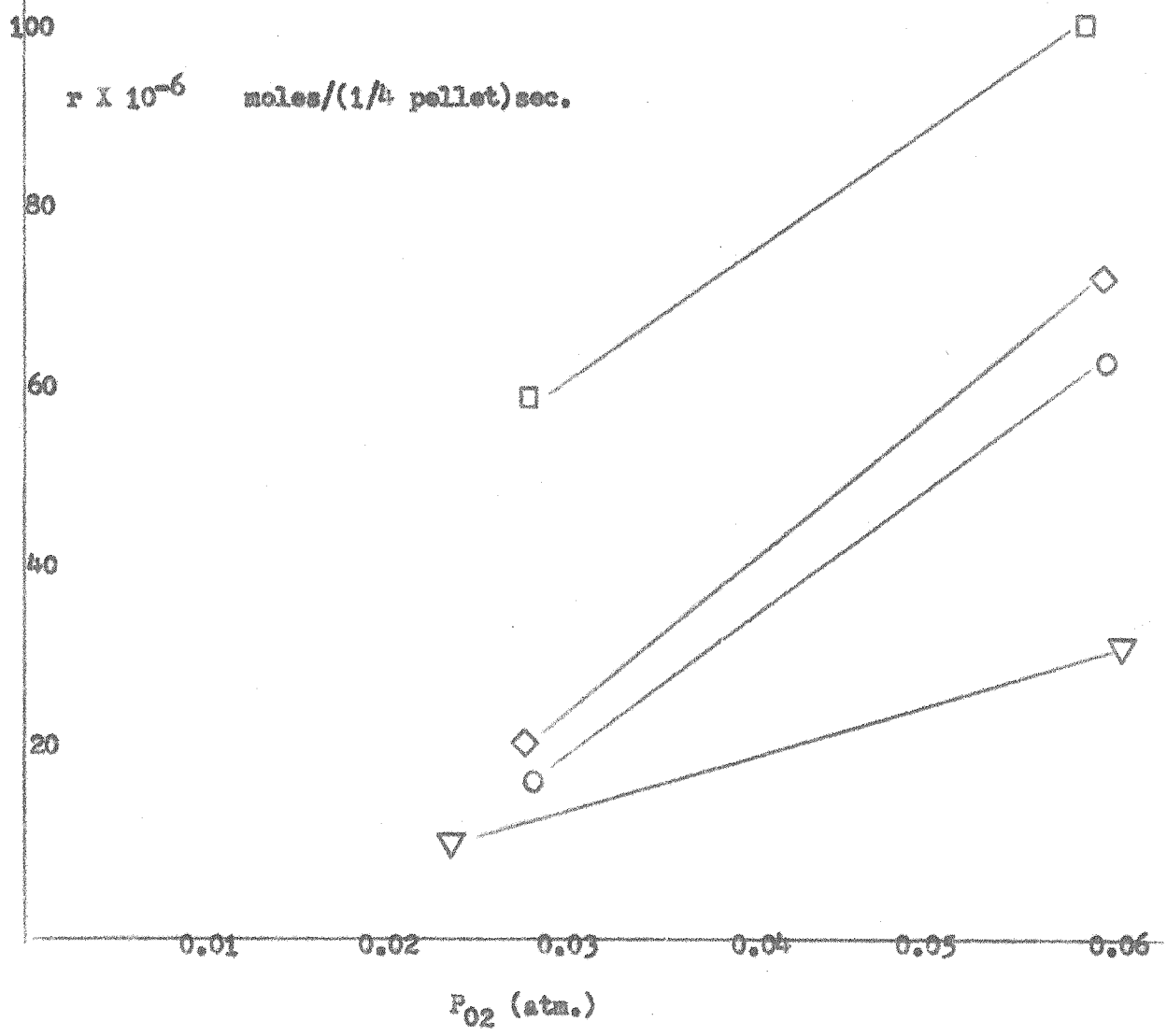


The activation energy of 10.8 kilo calories is quite close to that of Leder and Butt who reported  $10 \pm 2$  kilo calories as the activation energy for the Hinshelwood equation they defined in their data. These equations are illustrated in Figure 5 showing each of the above equations plotted as rate versus the partial pressure of oxygen. The rates are for node one of the pellet and thus, results in rates of reaction per  $1/4$  pellet or per  $1/2$  gram. In all cases the program calculated curves have steeper slopes than the rate curve defined by Maymo and Smith paper. At low partial pressures the rates are about the same for each equation but rates differ significantly at high partial pressures. Deviation is caused by the combined effects of the rate form being examined and the temperature variation of the data.

This problem also showed that the selection of specific rate forms have a major influence upon the percentage of reaction occurring in each node as a function of pellet radius. This was evidenced in the Maymo and Smith data as represented by the Hinshelwood equation proposed by Leder and Butt. The equilibrium constant (adsorption of oxygen) in the denominator of the rate equation increases rapidly with temperature, which would not happen if this specific constant was assumed zero and another one studied. This results in rate decreasing with temperature.

Since the temperature rises with distance into the pellet, the resultant decrease observed in rate might be explained by decreases in adsorbed oxygen. In view of this conclusion, a look at how the oxygen adsorption for platinum varies with temperature should be made.

| KEY | Reference | Equation  |
|-----|-----------|---|
| □   | Table II  | $r(1) = r_t$  |
| ◇   | Computer  | $r(1) = r_t - r(2) - r(3) - r(4)$   |
| ○   | Computer  | $r(1) = \frac{P_{O_2} P_{H_2}^2}{0.0123 \exp(\frac{10800}{RT}) + (639T - 2,600,000) P_{O_2}}$ |
| ▽   | (7)       | $r(1) = 0.655 P_{O_2}^{0.864} \exp(\frac{-5230}{RT})$   |



**FIGURE 5**  
 RATE VERSUS PARTIAL PRESSURE OF A  
 HYDROGEN OXYGEN CATALYSIS  
 OVER PLATINUM

It was found that adsorption rate decreases with temperature (2) according to the following equation:

$$\frac{dN}{dt} = \frac{P(1-\theta)}{(2\pi MKT)^{1/2}} - B\theta \quad (64)$$

Since this indicates the forward rate of oxygen adsorption is decreasing with temperature for equilibrium, the desorption rate must also decrease indicating a lower rate of product formation. From equation 64 a 30% to 40% decrease may occur for a 2 to 1 change in temperature but no change as great as that observed in the computer analysis. It is, therefore, believed that the large variation in this coefficient is unlikely.

## SECTION III

CONCLUSIONS

A computer program has been constructed that takes data from heterogeneous reactions, gas phase reaction with solid pellet catalyst, and for given mainstream compositions, pellet surface temperatures, catalyst properties, and reaction rates estimates the representative Hinshelwood rate equation. In the sample problem (hydrogen and oxygen catalyzed by platinum) the calculated equations for the first iteration exhibited a similar activation energy to that determined by authors of (7).

Equation: (7)

$$r = 0.655 \exp\left(-\frac{5230}{RT}\right) (P_{O_2}) \quad (65)$$

Computer Calculated Hinshelwood Equation:

$$r = \frac{P_{O_2} + P_{H_2}^2}{0.411 \exp\left(\frac{+6180}{RT}\right) + 1.66 \times 10^{11} \exp\left(\frac{-13100}{RT}\right) (P_{O_2})} \quad (66)$$

which at low values of  $P_{O_2}$  provides the following equation:

$$r = 2.4 \exp\left(\frac{-6180}{RT}\right) (P_{O_2}) (P_{H_2})^2 \quad (67)$$

The activation energy 6180 cal/mole is of similar magnitude to 5230 cal/mole in spite of the fact that rate forms assumed (first order versus Hinshelwood) were different. This rate form, however, did not fully explain the temperature characteristics of the system and the final equation had an activation energy of approximately 10.8 kilocalories more nearly agreeing with the  $10 \pm 2K$  calories observed for hydrogen oxygen over platinum study of (8).

A negative low temperature oxygen adsorption constant was obtained rejecting this equation.

The findings of the computer program are by no means conclusive but several observations are significant in determining the type of information which may be obtained.

First rate fractions (of total pellet rate) are defined for each node in each pellet. Applying the equations defining temperature drop and concentration variation as a function of node rates from Section 2 of Part E, temperature and concentration through the pellet may be calculated. From temperature and concentration versus radius plots, it is possible to determine how the rate equations affect the shape of these plots. This may be instrumental in selection of the representative rate mechanisms.

Such a result was inadvertently encountered when the temperature sensitivity of the Hinshelwood constants in the sample problem Part F produced decreases in rate as the temperature rose with distance into the pellet. While such decreases can occur as a result of changes in adsorption constants the abruptness of the change placed this rate form in doubt.

It is conjectured that when Hinshelwood rate equations represent the data, Kinetic phenomena controls rates at the pellet surface but as the reactant diffuses into the center, diffusion can control. Furthermore with variation in chemical reactant or product concentrations it is possible that further inside the pellet chemical rates may again control

rate. Such variations are not likely to be picked up by first order rate approximations but would be recognized in the node analyses.

This form of analysis, because of its sensitivity to these parameter variations can be more useful in selecting rate equations than other methods now in use.

The accuracy of the analyses performed is dependent upon the presence of accurate values for effective diffusivities and effective thermal conductivity. The node analysis can be made as accurate as required by increasing the number of nodes, obtaining data describing catalyst properties and by accurate measurement of chemical concentrations and reaction rates.

IV

RECOMMENDATIONS

The computer program in this study has been designed to give maximum freedom to the programmer for alteration as may be required for any heterogenous reaction. It is recommended that the computer program be made more accurate by decreasing size of iteration steps and by calling for the library sub-routine for simultaneous linear solutions of the rate equations for the Hinshelwood constants.

It is recommended that the computer program be used to study industrial reactor data and that the Hinshelwood rate equations from the pellet data be compared with previous correlations derived from particles or pellets. Results are expected to define areas where further experimental study may be profitable.

In general, it is felt that this computer program can act effectively in augmenting experimental investigations.

APPENDIX

COMPUTER PROGRAM INPUT AND OUTPUT CONSIDERATIONS

This discussion is designed to be a guide to utilizing the "Hinshelwood rate from catalyst data" computer program. In brief, this discussion considers the input data package and then some areas where hang-ups may occur. A nomenclature list summarizes the principal variables on pages

1. Input Considerations

First, it is noted that there are eleven dimension statements and one common statement. Matrices B and C are storage matrices. B and C contain the input data with fourteen bits of information used per data point. The term GC is the universal gas constant and is input in whatever dimensions the programmer wishes to use. The program is thus able to work in any set of dimensions but the programmer must make certain that the input data is in consistent dimensions.

The input data begins with the statement read 5, NO and continues for twelve statements to read 13, PM, PN.

Summary input parameters. The following outlines the data as input to the computer based upon an equilibrium equation of the reaction of the type  $A + B \rightarrow R + S$ .

- 1. NO - The number of cases (KK) or mechanisms to be run and specifies number of cards in the next sequence.



2. MW, MQ, MU, MY, TN, VO - The values MW through MZ define addresses in function routines used for rate mechanisms. MW is the address in the potential function of POTP; MQ the address of the A adsorption term in function routine KSORPA; MU is the address of the B adsorption term in KSORPB and likewise, MQ, MZ are addresses in the function sub-routines for defining adsorption terms R and S in KSORPR and KSORPS. The term TN indicates the power which the adsorption terms are raised. The term VO defines the terms that are to be used in the SOLV sub-routine. This accomplished by directing the computer to place terms generated from the least squares computation in matrix G or in matrix GV in the correct form for simultaneous linear equation solution. The equations are solved in subroutine SOLV. VO also is then used to define the value of the Hinshelwood constants that are returned from SOLV back to the main program. As may be noted from this sequence described above, potential program hang-up may have greatest chance of occurring in selection of the correct value of VO.

3. The terms MF and NF define the number of points to be placed in matrix B and matrix C. The two matrices are selected for use with two pellet surface temperatures observed. The values MF and NF also determine the number of input cards to follow. Since half the data per point is allotted to a card, the number of cards will be double that of MF and NF.

4 - 5. Matrix B(J,L1) and (J2, L2) input data. These matrices are doubly subscripted. The first number (J) representing a unit of data point and (L) representing the data point number. The first four values

of J are partial pressures or concentrations of component A, B, R and S. The fifth value is the total pellet rate. Terms J6 through 9 are the diffusion limits at nodes one, two, three, four defined by some fraction of the total rate for which diffusion may occur. That is  $RA(M)/A(5,M)$  RA representing diffusion rate which could reach node N from the next outermost node. The value  $A(5,M)$  is the total reaction rate which was input to matrix B or C. The last terms J10 to 13 are rate limits based upon combined rate equation and diffusion limits depending upon which is controlling the rate in each node two to four. The last column J14 is now stores surface temperature but may be used to store additional data if desired, since surface temperature is introduced in another input location.

6. The diffusion constant DE ( ) are values of diffusivities of species A, B, R and S representing best average value for the four nodes investigated. For greater accuracy it may be desirable to introduce an equation to correct diffusivities for varying node conditions.

7. Next, several constant RP -- pellet radius, CP gas-specific heat, HR heat of reaction and KE equilibrium constant are introduced.

8. Then temperatures applying to surface temperature of pellets matrix B is TS1 and for matrix C is TS2.

9. Another set of constants included are F, H and Q which are the node relation of species B, R and S to specie A.

$$(F = \frac{\text{moles B}}{\text{moles A}} \text{ for mass balance})$$

10. Additional information introduced includes the number of unknown constants to be solved for in the least squares solution (U2), the effective thermal conductivity of the pellet/gas combination (CK) and the universal gas constant (GC).

11. Values of FR and FD terms 2 to 4 indicate the allowable deviation of the sum of the concentrations in nodes two to four defined for the diffusion program.

12. Last, the values for the number of iterations per mechanism to be allowed in the calculations. It is estimated that convergence from initial estimate of total pellet reaction taking place in node one requires at least three iterations. Then, review of data and better initial estimates of node one rates should provide convergence more rapidly.

## II. Problem Areas Computer May Encounter

First, in providing the matrix GV which is subsequently sent to the subroutine SOLV. It is necessary to place the pertinent matrix terms in form such that unknowns appear in the first (U2) columns with the residual or known term column in (U2 + 1) column. Thus the subroutine mat has been used to move the pertinent variable to the correct matrix locations for solution. At present, mat does not have all the possible combinations and it may be necessary to add additional ones for GV sets to be evaluated. Similar considerations of output for the correct Hinshelwood coefficient from subroutine SOLV may be required.

It is possible that subroutine SOLV may bomb out if any of the coefficients being solved for go to zero at which point the subroutine

prints out the word "EXTOL" indicating a zero coefficient and the program will go to the next case NO(KK). Other than these locations, the program will probably run to completion unless a term exceeds the storage capacity of the computer.

The program has taken into consideration that Hinshelwood coefficients may be zero and to by-pass difficulties in being stopped at an early iteration because of difficulties in computing temperature correlation based upon Arrhenius equation. The subroutine temco computes either an Arrhenius or a linear relation and uses that for the next iteration. Thus the print-out of the Hinshelwood constants at the end of a run should be made to see if constants are negative. This is done by checking values printed out of the matrix E(2, 5) where values of AK and DB are listed. AK is the constant and DB is the exponential term (or slope in linear result)  $\exp(DB/RT)$ .

Output data. The program is designed to print out the final values of the terms in matrix A and B thus giving fractional rates in terms of diffusion limits and diffusion/rate limits combines. Also printed out is the coefficient of variation for the difference between node one rates and the equation derived rates. This is printed out of matrix COVNB(KK) and COVNC(KK). Further data is printed out of the AK and DB matrices which provide Arrhenius relation coefficients as indicated in the following equation:

$$K = (AK) \exp \left( \frac{DB}{RT} \right)$$

As a check on the validity of AK and DB is matrix E which provides the Hinshelwood coefficients for each matrix from which the Arrhenius coefficients have been calculated. From these data most pertinent results can be determined both in terms of individual nodes and node one versus rate equation comparisons. It may be of interest to store calculated rates and node one rates at the end of the last iteration for each matrix. This will undoubtedly require additional storage matrices.

NOMENCLATURE

(Computer)

COMPUTER PROGRAM

|             |   |
|-------------|---|
| MW          | Address in subroutine POTF  |
| MQ          | Address in subroutine KSORPA  |
| MV          | Address in subroutine KSORPB  |
| MY          | Address in subroutine KSORPR  |
| MZ          | Address in subroutine KSORPS  |
| TW          | Exponent of the adsorption term   |
| VO          | Designates addresses in subroutine MAT and SOLV   |
| A           | Matrix values used in working program   |
| B           | Matrix used to store data before use in matrix A  |
| C           | Matrix used to store data before use in matrix A  |
| E           | Matrix used to store Hinshelwood coefficients<br>(K1B...K5B) (K1C...K5C)  |
| EM          | Matrix used in subroutine TEMCO to store $K_1( ) \dots$<br>$K_5( )$   |
| AK          | Arrhenius coefficient   |
| DB          | Arrhenius coefficient in exponential term   |
| G and GV    | Matrices in which summation used in least squares<br>routine are held prior to simultaneous linear<br>equation solution |
| K(1)---K(6) | Constants returned by subroutine SOLV   |
| RA(n)       | Diffusion limited rate  |
| R(N)        | Node rates limited by both rate equation and<br>diffusion   |
| R1 calc (N) | Rates calculated from rate equation   |
| TA(n)       | Node temperatures   |

WK and YK      Temperature dependent constants calculated from Arrhenius equation  
 DR(N)          Distance between nodes (diffusion path)  
 AR(N)          Near area between node locations for heat and mass flow  
 CA(N) or PA    Concentration of species A for node N  
 CB(N) or PB    Concentration of species B for node N  
 CR(N) or PR    Concentration of species R for node N  
 CS(N) or PS    Concentration of species S for node N  
 NOTE: With "S" added to end -- stands for stream condition  
 FD(N)          Concentration sum node limit  
 FR(N)          Concentration sum node limit  
 KSORPA        Function subroutine A adsorption value  
 KSORPB        Function subroutine B adsorption value  
 KSORPR        Function subroutine R adsorption value  
 KSORPS        Function subroutine S adsorption value  
 MF            Number of data points in matrix B  
 NF            Number of data points in matrix C  
 RP            Pellet radius  
 CP            Specific heat of gas composition  
 HR            Heat of reaction  
 KE            Reaction equilibrium coefficient  
 K            Matrix storing values from solutions in SOLV subroutines  
 DEA    )  
 DEB    )      Diffusion coefficients of species A, B, R and S  
 DER    )  
 DES    )

|             |   |
|-------------|---|
| TS1 and TS2 | Surface temperatures of pellets whose data is supplied in matrix B and C respectively |
| F, H, and Q | Moles of B, R, or S involved in reaction per mole of A reacted                        |
| UZ          | Number of unknown in least square solution  |
| CK          | Effective thermal conductivity of pellet  |
| GC          | Universal gas constant  |
| FD and FR   | Limit of concentration of species summed at each node                                 |
| LP          | Indicator defining whether diffusion branch of program is to be run or not            |
| TIM         | Iteration counter in program matrix B   |
| TIN         | Iteration counter in program matrix C   |
| I           | Matrix B or C indicator   |
| IN          | Loop indicator  |
| M           | Data point indicator for working matrix   |
| ZD          | Multiplier for adjustment of rate equation in iteration process                       |
| IZ          | Indicator which prevents storage of rate values until ZD achieves satisfactory value  |
| COV( )      | Coefficient of variation (different endings with Location in program)                 |
| DEN         | The denominator of the rate equation containing the KSCR <sub>P</sub> terms           |
| SIGF        | Subroutine which checks sign of sums of concentrations                                |



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```

001 DIMENSION MW(9),MQ(9),MU(9),MY(9),MZ(9),TN(9),VC(9)
002 DIMENSION A(14,10),B(14,10),C(14,10)
003 DIMENSION E(2,5)
004 DIMENSION EM(5)
005 DIMENSION DB(5),AK(5)
006 DIMENSION G(5,6),GV(5,6),K(6)
007 DIMENSION R(4),RA(4),RCALC(4),TA(4),WK(4),YK(4),DR(4),AR(4)
008 DIMENSION CA(4),CB(4),CR(4),CS(4)
009 DIMENSION FD(4),FR(4)
010 DIMENSION CCVNB(9),CCVNC(9)
011 DIMENSION D(4)
012 REAL MW,MQ,MU,MY,MZ
013 REAL KE
014 REAL K1B,K2B,K3B,K4B,K5B,K1C,K2C,K3C,K4C,K5C
015 REAL KSCRPA,KSCRPB,KSCRPR,KSORPS
016 REAL K
017 READ 5,NO
018 READ 4,(MW(KK),MQ(KK),MU(KK),MY(KK),MZ(KK),TN(KK),VO(KK),KK=1,NO
019 READ 15,MF,NF
020 DO 6 L1=1,MF
021 6 READ( 1,106) (B(J,L1),J=1,14)
022 DO 10 L2=1,NF
023 10 READ( 1,106) (C(J2,L2),J2=1,14)
024 7 READ 12,DEA,DEB,DER,DES
025 8 READ 12,RP,CP,HR,KE
026 9 READ 13,TS1,TS2
027 READ 14,F,H,Q
028 READ 14,L2,CK,GC
029 READ 13,(FD(LD),FR(LD),LD=2,4)
030 READ 13,FM,FN
031 4 FORMAT(7F4.0)
032 5 FORMAT(112)
033 11 FORMAT(6F4.0)
034 12 FORMAT(4E10.3)
035 13 FORMAT(2F10.2)
036 14 FORMAT(3E10.3)
037 15 FORMAT(2I4)
038 75 FORMAT(1X,27H HINSHELWOOD RATE MECHANISM//,7F10.3)
039 76 FORMAT(1X,9H MATRIX B,(7E12.3))
040 77 FORMAT(14H DIFFUSIVITIES//,4E10.3)
041 78 FORMAT(1X,2H F,E10.3,5X,2H H,E10.3,5X,2H Q,E10.3)
042 79 FORMAT(1X,3H RP,E10.3,3X,3H CP,E10.3,3X,3H HR,E10.3,3H KE,E10.3)
043 80 FORMAT(7//1X,3H U2,E10.3,10X,3H CK,E10.3,10X,3H GC,E10.3)
044 81 FORMAT(//1X,10H ITERATION,2F10.2)
045 82 FORMAT(1X//1X,6H CCVNB,2E15.3)
046 83 FORMAT(1X//1X,9H MATRIX E,5E10.3,//1X,3H AK,5E10.3,3H DB,5E10.3)
047 84 FORMAT(1X,9H MATRIX C//,(7E12.3))
048 106 FORMAT(7E10.3)
049 DO 40 KK=1,NO

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0050      40  PRINT 75,MW(KK),MQ(KK),MU(KK),MY(KK),MZ(KK),TN(KK),VO(KK)
0051          DO 41  L1=1,MF
0052      41  PRINT 76,(B(J,L1),J=1,14)
0053          DO 42  L2=1,NF
0054      42  PRINT 84,(C(J2,L2),J2=1,14)
0055          PRINT 77,DEA,DEB,DER,DES
0056          PRINT 79,RP,CP,HR,KE
0057          PRINT 78,F,H,Q
0058          PRINT 80,U2,CK,GC
0059          PRINT 81,FM,FN
0060      98  KK=1
0061          LP=1
0062      99  N=TN(KK)
0063          LC=MQ(KK)
0064          LD=MW(KK)
0065          LF=MU(KK)
0066          LG=MY(KK)
0067          LH=MZ(KK)
0068          TIM=C.O
0069          TIN=C.C
0070      100  IN = 1
0071          ZD=1.0
0072          IZ=1
0073      101  I = 1
0074          VOK=VO(KK)
0075          NE=MF
0076          EN=MF
0077      107  J = 1
0078          L1 = 1
0079      109  KJ=J
0080      110  M=L1
0081          A(KJ,M) =B(J,L1)
0082          J=J+1
0083      111  IF(J-14) 109,109,112
0084      112  J = 1
0085          L1 = L1 + 1
0086          IF(L1-MF) 109,109,114
0087      114  IF(IN-2) 200,299,599
0088      115  I = 2
0089          VOK=VO(KK)
0090          NE=NF
0091          EN=NF
0092      119  J2 = 1
0093          L2 = 1
0094      120  KJ=J2
0095          M = L2
0096      121  A(KJ,M)=C(J2,L2)
0097          J2 = J2 + 1
0098      122  IF(J2-14) 120,120,123

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0099      123      J2 =1
0100              L2 = L2 + 1
0101              IF(L2-NF)120,120,125
0102      125      IF(IN-2) 200,299,599
0103      200      SUMV=C
0104              SUMVA1=0
0105              SUMVA2 =0
0106              SUMVA3=0
0107              SUMVA4=C
0108              SUMA1=C
0109              SUMA2=C
0110              SUMA3=0
0111              SUMA4=C
0112              SUMA1X=0
0113              SUMA12=C
0114              SUMA13=C
0115              SUMA14=C
0116              SUMA2X=0
0117              SUMA23=0
0118              SUMA24=C
0119              SUMA3X=C
0120              SUMA34=C
0121              SUMA4X=C
0122      201      DO 221 M=1,NE
0123              PA = A(1,M)
0124              PB = A(2,M)
0125              PR = A(3,M)
0126              PS = A(4,M)
0127              A1=KSORPA(LC,PA,PB,PR,PS,KE)
0128              A2=KSORPB(LF,PA,PB,PR,PS,KE)
0129              A3=KSORPK(LG,PA,PB,PR,PS,KE)
0130              A4=KSORPS(LH,PA,PB,PR,PS,KE)
0131              PT=POT(LD,PA,PB,PR,PS,KE)
0132              V=(PT/(A(5,M)*A(10,M)*ZD))**(1.0/N)
0133              SUMV=SUMV+V
0134      203              VA1 = V*A1
0135              SUMVA1=SUMVA1+VA1
0136      204              VA2 = V*A2
0137              SUMVA2=SUMVA2+VA2
0138      205              VA3 = V*A3
0139              SUMVA3=SUMVA3+VA3
0140      206              VA4 = V*A4
0141              SUMVA4=SUMVA4+VA4
0142      207              SUMA1=SUMA1+A1
0143      208              SUMA2=SUMA2+A2
0144      209              SUMA3=SUMA3+A3
0145      210              SUMA4=SUMA4+A4
0146      211              A1X = A1 **2
0147              SUMA1X=SUMA1X+A1X

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0148      212      A12 = A1 *A2
0149              SUMA12=SUMA12+A12
0150      213      A13 = A1*A3
0151              SUMA13=SUMA13+A13
0152      214      A14 = A1*A4
0153              SLMA14=SLMA14+A14
0154      215      A2X = A2**2
0155              SLMA2X=SUMA2X+A2X
0156      216      A23 = A2*A3
0157              SLMA23=SUMA23+A23
0158      217      A24 = A2*A4
0159              SLMA24=SUMA24+A24
0160      218      A3X = A3**2
0161              SUMA3X=SUMA3X+A3X
0162      219      A34 = A3*A4
0163              SLMA34=SUMA34+A34
0164      220      A4X = A4**2
0165      221      SUMA4X=SUMA4X+A4X
0166              G(1,1)=EN
0167              G(2,1)=SUMA1
0168              G(3,1)=SUMA2
0169              G(4,1)=SUMA3
0170              G(5,1)=SUMA4
0171              G(1,2)=SUMA1
0172              G(2,2)=SUMA1X
0173              G(3,2)=SUMA12
0174              G(4,2)=SUMA13
0175              G(5,2)=SUMA14
0176              G(1,3)=SUMA2
0177              G(2,3)=SUMA12
0178              G(3,3)=SUMA2X
0179              G(4,3)=SUMA23
0180              G(5,3)=SUMA24
0181              G(1,4)=SLMA3
0182              G(2,4)=SUMA13
0183              G(3,4)=SUMA23
0184              G(4,4)=SUMA3X
0185              G(5,4)=SUMA34
0186              G(1,5)=SUMA4
0187              G(2,5)=SUMA14
0188              G(3,5)=SUMA24
0189              G(4,5)=SUMA34
0190              G(5,5)=SUMA4X
0191              G(1,6)=SUMV
0192              G(2,6)=SUMVA1
0193              G(3,6)=SUMVA2
0194              G(4,6)=SUMVA3
0195              G(5,6)=SUMVA4
0196              IF(VOK=1) 222,224,224

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0197      222  CALL SOLVIG,VOK,U2,TCLR,K)
0198          IF(K(6)-1) 223,223,617
0199      223  IF(I-1) 226,226,227
0200      224  CALL NAT(G,VOK,GV)
0201          CALL SOLV(GV,VOK,U2,TCLR,K)
0202          IF(K(6)-1) 225,225,617
0203      225  IF(I-1) 226,226,227
0204      226  K1B=K(1)
0205          K2B=K(2)
0206          K3B=K(3)
0207          K4B=K(4)
0208          K5B=K(5)
0209          I=2
0210          GO TO 115
0211      227  K1C=K(1)
0212          K2C=K(2)
0213          K3C=K(3)
0214          K4C=K(4)
0215          K5C=K(5)
0216          E(1,1)=K1B
0217          E(2,1)=K1C
0218          E(1,2)=K2B
0219          E(2,2)=K2C
0220          E(1,3)=K3B
0221          E(2,3)=K3C
0222          E(1,4)=K4B
0223          E(2,4)=K4C
0224          E(1,5)=K5B
0225          E(2,5)=K5C
0226          DO 233 NL=1,5
0227      229  IF(E(2,NL)) 231,231,230
0228      230  IF(E(1,NL)) 231,231,232
0229      231  AK(NL)=(E(2,NL)-E(1,NL))/(TS2-TS1)
0230          DB(NL)=E(1,NL)-AK(NL)*TS1
0231          GO TO 233
0232      232  DB(NL)= GC*(TS1*TS2)/(TS1-TS2)*ALOG(E(1,NL)/E(2,NL))
0233          AK(NL)=E(1,NL)*EXP(DB(NL)/(GC*TS1))
0234      233  CONTINUE
0235      246  TS=TS1
0236          I=1
0237          GO TO 248
0238      247  TS=TS2
0239      248  CALL TEMCO(E,TS,AK,DB,EM)
0240          K(1)=EM(1)
0241          K(2)=EM(2)
0242          K(3)=EM(3)
0243          K(4)=EM(4)
0244          K(5)=EM(5)
0245          DO 280 NL=1,5

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0246      280 PRINT 281,AK(NL),DB(NL)
0247      281   FORMAT(4H AK,E10.3,4H DB,E10.3)
0248      249   SUMCC=C
0249      250   DO 255 M=1,NE
0250      PA =A(1,M)
0251      PB = A(2,M)
0252      PR = A(3,M)
0253      PS = A(4,M)
0254      A1=KSORPA(LC,PA,PB,PR,PS,KE)
0255      A2=KSORPB(LF,PA,PB,PR,PS,KE)
0256      A3=KSORPR(LG,PA,PB,PR,PS,KE)
0257      A4=KSORPS(LH,PA,PB,PR,PS,KE)
0258      PT=PUT(LD,PA,PB,PR,PS,KE)
0259      DEN=(K(1)+K(2)*A1+K(3)*A2+K(4)*A3+K(5)*A4)**N
0260      V=(PT/(A(5,M)*A(10,M)*ZD))**(1.0/N)
0261      RC=A(5,M)*A(10,M)*ZD
0262      IF(DEN-C.1*V)251,252,252
0263      251   IF(DEN+C.1*V) 252,252,253
0264      252   RCAL=PT/DEN
0265      GO TO 254
0266      253   RCAL =PT/(0.1*V)
0267      254   CC=(RCAL-RC)**2
0268      255   SUMCC =SUMCC + CC
0269      COV=(SUMCC/EN)**0.5
0270      256   IF(I = 1 ) 257,257,259
0271      257   COVB = COV
0272      PRINT 258,COVB
0273      258   FORMAT(5H COVB,E10.3)
0274      I=2
0275      GO TO 247
0276      259   COVC=COV
0277      PRINT 260,CVC
0278      260   FORMAT(5H COVC,E10.3)
0279      282   IN=2
0280      GO TO 101
0281      299   IF(LP-1) 300,300,399
0282      300   M=1
0283      DR(2)=0.1037*RP
0284      DR(3)=0.141*RP
0285      DR(4)=0.315*RP
0286      AR(2)=12.53*C.953*C.848*RP**2
0287      AR(3)=12.53*C.848*0.7076*RP**2
0288      AR(4)=12.53*0.7076*C.315*RP**2
0289      301   CAS=A(1,M)
0290      CBS=A(2,M)
0291      CRS=A(3,M)
0292      CSS=A(4,M)
0293      DO 309 MR=2,4
0294      RA(MR)=A(5,M)

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0295      302  CA(MR)=-RA(MR)*DR(MR)/(DEA*AR(MR))+CAS
0296      CB(MR)=-F*RA(MR)*DR(MR)/(DEB*AR(MR))+CBS
0297      CR(MR)=H*RA(MR)*DR(MR)/(DER*AR(MR))+CRS
0298      CS(MR)=Q*RA(MR)*DR(MR)/(DES*AR(MR))+CSS
0299      CALL SIGF( CA,CB,CR,CS,IK)
0300      IF(IK-1) 303,303,304
0301      303  RA(MR)=C.95*RA(MR)
0302      GO TO 302
0303      304  SUMC =CA(MR)+CB(MR)+CR(MR)+CS(MR)
0304      PRINT 311,SUMC
0305      IF(FD(MR)-SUMC) 305,306,306
0306      305  RA(MR)=C.95*RA(MR)
0307      GO TO 302
0308      306  IF(FR(MR)-SUMC) 308,308,307
0309      307  RA(MR)=C.95*RA(MR)
0310      GO TO 302
0311      308  CAS=CA(MR)
0312      CBS=CB(MR)
0313      CRS=CR(MR)
0314      CSS=CS(MR)
0315      309  CONTINUE
0316      A(7,M)=RA(2)/A(5,M)
0317      A(8,M)=RA(3)/A(5,M)
0318      A(9,M)= RA(4)/A(5,M)
0319      PRINT 311,A(7,M)
0320      311  FORMAT(3H A7,E1C.3)
0321      M=M+1
0322      IF(M-NE) 301,301,310
0323      310  IF(I-1)325,325,328
0324      325  DO 326 M=1,NE
0325      B(7,M)=A(7,M)
0326      B(8,M)=A(8,M)
0327      B(9,M)=A(9,M)
0328      326  CONTINUE
0329      GO TO 115
0330      328  DO 329 M=1,NE
0331      C(7,M)=A(7,M)
0332      C(8,M)=A(8,M)
0333      C(9,M)=A(9,M)
0334      329  CONTINUE
0335      330  LP=2
0336      GO TO 101
0337      399  M=1
0338      400  IF(I-1) 401,401,402
0339      401  TSA=TS1
0340      GO TO 403
0341      402  TSA=TS2
0342      403  RD1=A(5,M)
0343      RD2=A(5,M)*A(7,M)

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C344      RD3=A(5,M)*A(8,M)
C345      RD4=A(5,M)*A(9,M)
C346      R(1)=A(5,M)-KD2
C347      R(2)=RD2-RD3
C348      R(3)=RD3-RD4
C349      R(4)=RD4
C350      404 DT2=DR(2)*(R(2)+R(3)+R(4))*HR/(CK*AR(2))
C351      DT3=DR(3)*(R(3)+R(4))*HR/(CK*AR(3))
C352      DT4=DR(4)*(R(4))*HR/(CK*AR(4))
C353      405 TA(1)=TSA
C354      TA(2)=TSA+DT2
C355      TA(3)=TA(2)+DT3
C356      TA(4)=TA(3)+DT4
C357      496 CAS=A(1,M)
C358      CBS=A(2,M)
C359      CRS=A(3,M)
C360      CSS=A(4,M)
C361      497 DU 505 ML=2,4
C362      DU501 LK=1,5
C363      IF(E(1,LK)) 499,499,498
C364      498 IF(E(2,LK)) 499,499,500
C365      499 WK(LK)=AK(LK)*IA(ML)+DE(LK)
C366      GO TO 501
C367      500 WK(LK)=AK(LK)*EXP(-DB(LK)/(GC*TA(ML)))
C368      501 CONTINUE
C369      D(2)=R(2)+R(3)+R(4)
C370      D(3)=R(3)+R(4)
C371      D(4)=R(4)
C372      PA=-D(ML)*DR(ML)/(DEA*AR(ML))+CAS
C373      PB=-F*D(ML)*DR(ML)/(DEB*AR(ML))+CBS
C374      PR=H*D(ML)*DR(ML)/(DER*AR(ML))+CRS
C375      PS=Q*D(ML)*DR(ML)/(DES*AR(ML))+CSS
C376      A1=KSORPA(LC,PA,PB,PR,PS,KE)
C377      A2=KSORPB(LF,PA,PB,PR,PS,KE)
C378      A3=KSORPK(LG,PA,PB,PR,PS,KE)
C379      A4=KSORPS(LH,PA,PB,PR,PS,KE)
C380      SRA=A1*WK(2)
C381      SRB=A2*WK(3)
C382      SKR=A3*WK(4)
C383      SRS=A4*WK(5)
C384      PT=POT(LD,PA,PB,PR,PS,KE)
C385      CAS=PA
C386      CBS=PB
C387      CRS=PR
C388      CSS=PS
C389      DEN=(WK(1)+SRA+SRB+SRR+SRS)
C390      V=(PT/(A(5,M)*A(10,M)*ZD))**(1.0/N)
C391      IF(DEN-0.1*V) 502,504,504
C392      502 IF(DEN+0.1*V) 504,504,503

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C393      503      RCALC(MI)=PT/(O.1*V)
C394      GO TO 505
C395      504      RCALC(MI)=PT/DEN
C396      505      CONTINUE
C397      506      IF(RCALC(2)-R(2)) 512,507,507
C398      507      IF(RCALC(3)-R(3)) 513,508,508
C399      508      IF(RCALC(4)-R(4)) 514,509,509
C400      509      IF(RD2-R(2)-R(3)-R(4)) 512,510,510
C401      510      IF(RD3-R(3)-R(4)) 513,511,511
C402      511      IF(RD4-R(4)) 514,515,515
C403      512      R(2)=C.8*R(2)
C404      GO TO 404
C405      513      R(3)=0.8*R(3)
C406      R(2)=R(2)+C.2*(R(3)/C.8)
C407      GO TO 404
C408      514      R(4)=R(4)*C.8
C409      R(3)=R(3)+C.2*(R(4)/O.8)
C410      GO TO 404
C411      515      R(1)=A(5,M)-R(2)-R(3)-R(4)
C412      PRINT 406,R(3)
C413      406      FORMAT(3H'R3,E10.3)
C414      IF(A(5,M)*A(10,M)*Z0-R(1)) 517,517,516
C415      516      Z0=0.8*Z0
C416      IN=1
C417      GO TO 101
C418      517      IF(IZ-1) 518,518,521
C419      518      M=M+1
C420      IF(M-NE)400,400,519
C421      519      IF(I-1) 115,115,520
C422      520      IZ=2
C423      GO TO 101
C424      521      IF(I-1) 522,522,523
C425      522      B(10,M)=R(1)/A(5,M)
C426      B(11,M)=R(2)/A(5,M)
C427      B(12,M)=R(3)/A(5,M)
C428      B(13,M)=R(4)/A(5,M)
C429      B(14,M)=TA(Z)
C430      GO TO 524
C431      523      C(10,M)=R(1)/A(5,M)
C432      C(11,M)=R(2)/A(5,M)
C433      C(12,M)=R(3)/A(5,M)
C434      C(13,M)=R(4)/A(5,M)
C435      C(14,M)=TA(Z)
C436      524      M=M+1
C437      IF(M-NE) 400,400,526
C438      526      IF(I-1) 527,527,530
C439      527      GO TO 115
C440      530      IN=3
C441      GO TO 101

```

CRTRAN IV MODEL 44 PS VERSION 3, LEVEL I DATE 69119

```

C442      599      SUMCOR=C
C443              DO 607 M=1,NE
C444              IF(I=1) 600,600,601
C445      600      TS=TS1
C446              GO TO 602
C447      601      IS=TS2
C448      602      PA=A(1,M)
C449              PB=A(2,M)
C450              PR=A(3,M)
C451              PS=A(4,M)
C452              CALL TEMCO(E,TS,AK,DB,EM)
C453              YK(1)=EM(1)
C454              YK(2)=EM(2)
C455              YK(3)=EM(3)
C456              YK(4)=EM(4)
C457              YK(5)=EM(5)
C458              A1=KSORPA(LC,PA,PB,PR,PS,KE)
C459              A2=KSORPB(LF,PA,PB,PR,PS,KE)
C460              A3=KSORPR(LG,PA,PB,PR,PS,KE)
C461              A4=KSORPS(LH,PA,PB,PR,PS,KE)
C462              PT=PCT(LD,PA,PB,PR,PS,KE)
C463              SPA=A1*YK(2)
C464              SPB=A2*YK(3)
C465              SPR=A3*YK(4)
C466              SPS=A4*YK(5)
C467              DEN=(YK(1)+SPA+SPB+SPR+SPS)**N
C468              R1=A(5,M)*A(10,M)
C469              V=(PT/(A(5,M)*A(10,M)))**((1.0/N)
C470              IF(DEN-C.1*V) 603,605,605
C471      603      IF(DEN+C.1*V) 605,605,604
C472      604      R1CALC=PT/(0.1*V)
C473              GO TO 606
C474      605      R1CALC=PT/DEN
C475              PRINT 629,R1CALC,R1
C476      606      CDK=(R1CALC-R1)**2
C477      607      SUMCDR=SUMCCR+CDK
C478              COVAR=SQRT(SUMCCR/EN)
C479              PRINT 616,COVAR
C480      616      FORMAT(6H COVAR,E10.3)
C481      608      IF(I-1)609,609,612
C482      609      COVIB=2.0*COVB
C483              COVNB(KK)=COVAR
C484              IF(COVIB-COVAR) 610,610,611
C485      610      IN=1
C486              TIM=TIM+1
C487              IF(TIM-FM) 100,617,617
C488      611      GO TO 115
C489      612      COVIC=2.0*COVC
C490              COVNC(KK)=COVAR

```

ORTRAN IV MODEL 44 PS VERSION 3, LEVEL I DATE 69119

```
0491      IF(COVIC=COVAR)613,613,614
0492      613      IN=1
0493      TIN=TIN+1
0494      IF(TIN-FN) 100,617,617
0495      614      CONTINUE
0496      617      DO 618      L1=1,MF
0497      DO 618      J=1,I4
0498      618      PRINT 76,B(J,L1)
0499      619      PRINT 83,E,AK,DB
0500      DO 620      M=1,MF
0501      620      B(1C,M)=1.C
0502      DO 621      L2=1,NF
0503      DO 621      J2=1,I4
0504      621      PRINT 84,C(J2,L2)
0505      DO 622      M=1,NF
0506      622      C(1C,M)=1.C
0507      624      KK=KK+1
0508      IF(KK-NO) 99,99,625
0509      625      DO 626      KK=1,NC
0510      626      PRINT 82,COVN3(KK),CCVNC(KK)
0511      629      FORMAT(7H'RICALC',E10.3,5X,3H'R1',E10.3)
0512      STOP
0513      END
```

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```
0001          FUNCTION POT(LD,PA,PB,PR,PS,KE)
0002          REAL KE
0003          GO TO (151,152,153,154,156,157,158,159,160),LD
0004          151 POT=0
0005          GO TO 160
0006          152 POT=PA-PR/KE
0007          GO TO 160
0008          153 POT=PA-(PR*PS)/KE
0009          GO TO 160
0010          154 POT=(PA/PS)-(PR/KE)
0011          GO TO 160
0012          156 POT= PA*PR-PR/KE
0013          GO TO 160
0014          157 POT=PA*PB**2-PR/KE
0015          GO TO 160
0016          158 POT=PA*PB-PR/KE
0017          GO TO 160
0018          159 POT=PA*PB-PR*PS/KE
0019          160 RETURN
0020          END
```

CRTRAN IV MODEL 44 PS VERSION 3, LEVEL 1 DATE 69119

```
0001 REAL FUNCTION KSORPA(LC,PA,PB,PR,PS,KE)
0002 REAL KE
0003 GO TO(171,172,173,174,175,176,177,178,179,180,181,182),LC
0004 171 KSORPA=C
0005 GO TO 182
0006 172 KSORPA=PR/KE
0007 GO TO 182
0008 173 KSORPA=(PA)**(1/2)
0009 GO TO 182
0010 174 KSORPA=(PR*PS)/KE
0011 GO TO 182
0012 175 KSORPA=(PR/KE)**(1/2)
0013 GO TO 182
0014 176 KSORPA=(PR*PS/KE)**(1/2)
0015 GO TO 182
0016 177 KSORPA=PR/(KE*PB)
0017 GO TO 182
0018 178 KSORPA=(PR/(KE*PB))**(1/2)
0019 GO TO 182
0020 179 KSORPA= PR*PS/(KE*PB)
0021 GO TO 182
0022 180 KSORPA=( PR*PS/(KE*PB))**(1/2)
0023 GO TO 182
0024 181 KSORPA= PA
0025 182 RETURN
0026 END
```

CRTRAN IV MODEL 44 PS VERSION 3, LEVEL I DATE 69119

```
0001 REAL FUNCTION KSORPB(LF,PA,PB,PR,PS,KE)
0002 REAL KE
0003 GO TO (184,185,186,187),LF
0004 184 KSORPB=C
0005 GO TO 188
0006 185 KSORPB=PR/(KE*PA)
0007 GO TO 188
0008 186 KSORPB=PR*PS/(KE*PS)
0009 GO TO 188
0010 187 KSORPB=PB
0011 188 RETURN
0012 END
```

ORTRAN IV MODEL 44 PS VERSION 3, LEVEL 1 DATE 69119

```
0001 REAL FUNCTION KSCRPR(LG,PA,PB,PR,PS,KE)
0002 REAL KE
0003 GO TO (189,190,191,192,193,194) ,LG
0004 189 KSORPR=PR
0005 GO TO 195
0006 190 KSORPR=0
0007 GO TO 195
0008 191 KSCRPR=KE*PA
0009 GO TO 195
0010 192 KSCRPR=KE*PA/PS
0011 GO TO 195
0012 193 KSORPR=KE*PA*PB
0013 GO TO 195
0014 194 KSORPR=KE*PA*PB/PS
0015 195 RETURN
0016 END
```

CRTRAN IV MODEL 44 PS VERSION 3, LEVEL 1 DATE 69119

```
C001 REAL FUNCTION KSCRPS(LH,PA,PE,PR,PS,KE)
C002 REAL KE
C003 GO TO (197,198), LH
C004 197 KSORPS=PS
C005 GO TO 199
C006 198 KSORPS=0
C007 199 RETURN
C008 END
```



FORTRAN IV MODEL 44 PS VERSION 3, LEVEL I DATE 69119

```
0001      SUBROUTINE SIGF(CA,CB,CR,CS,/IK/)
0002      IF(CA-C) 700,697,697
0003      697  IF(CB-C) 700,698,698
0004      698  IF(CR-0) 700,699,699
0005      699  IF(CS-C) 700,701,701
0006      700  IK=1
0007      GO TO 702
0008      701  IK=2
0009      702  RETURN
0010      END
```

ORTRAN IV MODEL 44 PS VERSION 3, LEVEL 1 DATE 69119

```
0001      SUBROUTINE TEMCC(E,TS,AK,DB,/EM/)
0002      GC=1.98
0003      DIMENSION E(2,5),AK(5),DB(5),EM(5)
0004      1      DO 5 MV=1,5
0005      IF(E(1,MV)) 3,3,2
0006      2      IF(E(2,MV)) 3,3,4
0007      3      EM(MV)=AK(MV)*TS+DB(MV)
0008      GO TO 5
0009      4      EM(MV)=AK(MV)*EXP(-DB(MV)/(GC*TS))
0010      5      CONTINUE
0011      6      RETURN
0012      END
```

0001 SUBROUTINE MAT(G,VCK,/GV/)

0002 DIMENSION G(5,6)

0003 DIMENSION GV(5,6)

0004 KP=VCK

0005 GO TO (1,2,3,4),KP

0006 1 GV(1,1)=G(1,1)

0007 GV(2,1)=G(2,1)

0008 GV(3,1)=G(3,1)

0009 GV(1,2)=G(1,2)

0010 GV(2,2)=G(2,2)

0011 GV(3,2)=G(3,2)

0012 GV(1,3)=G(1,3)

0013 GV(2,3)=G(2,3)

0014 GV(3,3)=G(3,3)

0015 GV(2,4)=G(2,6)

0016 GV(3,4)=G(3,6)

0017 2 GV(1,1)=G(1,1)

0018 GV(2,1)=G(2,1)

0019 GV(3,1)=G(3,1)

0020 GV(4,1)=G(4,1)

0021 GV(1,2)=G(1,2)

0022 GV(2,2)=G(2,2)

0023 GV(3,2)=G(3,2)

0024 GV(4,2)=G(4,2)

0025 GV(5,2)=G(5,2)

0026 GV(1,3)=G(1,3)

0027 GV(2,3)=G(2,3)

0028 GV(3,3)=G(3,3)

0029 GV(4,3)=G(4,3)

0030 GV(1,4)=G(1,4)

0031 GV(2,4)=G(2,4)

0032 GV(3,4)=G(3,4)

0033 GV(4,4)=G(4,4)

0034 GO TO 5

0035 3 GV(1,1)=G(1,1)

0036 GV(2,1)=G(2,1)

0037 GV(1,2)=G(1,2)

0038 GV(2,2)=G(2,2)

0039 GV(1,3)=G(1,6)

0040 GV(2,3)=G(2,6)

0041 GO TO 5

0042 4 GV(1,1)=G(1,1)

0043 GV(2,1)=G(3,1)

0044 GV(1,2)=G(1,3)

0045 GV(2,2)=G(3,3)

0046 GV(1,3)=G(1,6)

0047 GV(2,3)=G(3,6)

0048 5 RETURN

0049 END

CRTRAN IV MODEL 44 PS VERSION 3, LEVEL I DATE 69119

```

0001      SUBROUTINE SOLV(A,VCK,U2,TCLR,/K/)
0002      DIMENSION A(5,6),K(6)
0003      REAL K
0004      N2=U2
0005      N1=N2+1
0006      DO 14 I=1,N2
0007      DIAG=A(I,I)
0008      IF(DIAG) 5,25,5
0009      5 DO 6 J=1,N1
0010      6 A(I,J)=A(I,J)/DIAG
0011      KJ=1
0012      9 IF(KJ-I) 11,13,11
0013      11 FCTR=A(KJ,I)
0014      DO 12 J=1,N1
0015      12 A(KJ,J)=A(KJ,J)-FCTR*A(I,J)
0016      13 KJ=KJ+1
0017      IF(KJ=N2) 9,9,14
0018      14 CONTINUE
0019      IF(VCK=1) 20,20,21
0020      20 K(1)=A(1,6)
0021      K(2)=A(2,6)
0022      K(3)=A(3,6)
0023      K(4)=C
0024      K(5)=C
0025      K(6)=1
0026      21 IF(VCK=3) 22,23,24
0027      22 K(1)=A(1,5)
0028      K(2)=A(2,5)
0029      K(3)=A(3,5)
0030      K(4)=A(4,5)
0031      K(5)=C
0032      K(6)=1
0033      GO TO 27
0034      23 K(1)=A(1,3)
0035      K(2)=A(2,3)
0036      K(3)=C
0037      K(5)=C
0038      K(6)=1
0039      GO TO 27
0040      24 K(1)=A(1,3)
0041      K(2)=C
0042      K(3)=A(2,3)
0043      K(4)=C
0044      K(5)=C
0045      K(6)=1
0046      GO TO 27
0047      19 FORMAT(E13.2)
0048      25 PRINT 26,A(I,I)
0049      K(6)=2

```

CRTRAN IV MODEL 44 PS VERSION 3, LEVEL 1 DATE 69119

C050 26 FORMAT (6H EXTCL,EIC.3)  
C051 27 RETURN  
C052 END

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