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# Bio-mechanics of the hip joint and the engineering considerations in the treatment of unstable intertrochanteric fractures

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# ABSTRACT

Title of Thesis: Bio-Mechanics of the Hip-Joint and the Engineering Considerations in the Treatment of Unstable Intertrochanteric Fractures

Manoj D. Nene, M. S. Engineering, October 1991

Thesis directed by: Dr. Raj S. Sodhi

Numerous previous attempts have been made to determine the magnitude and the direction of forces acting on the hip joint. The mechanism of femoral neck fractures and the frequently occurring failure of its internal fixation has led engineers to analyze the forces involved. An unstable intertrochanteric fracture is one which lacks continuity of the bone cortex on the opposing surfaces of the proximal and digital fragments. A mathematical model is created in this study to examine the 135° and 150° nail plate. The results give an approximate estimation of stresses on the two plates. A 3D finite element model of the two plates is created and the plate is loaded with different forces. Stress analysis of the two plates is performed to obtain the optimum design for an intertrochanteric fracture fixation device. A study is also made of the variables affecting the treatment of Unstable Intertrochanteric Fractures. This study concludes that the location of the plate and the plate angle affect the stresses as well as the treatment of the fractures. From the study we can conclude that the 150° plate is better than the 135° plate, since the stresses found in the 150° plate were calculated to be lower than the 135° plate.

## $\left(\frac{d}{d}\right)$  BIO-MECHANICS OF THE HIP JOINT AND THE ENGINEERING **CONSIDERATIONS IN THE TREATMENT OF UNSTABLE INTERTROCHANTERIC FRACTURES**

by  $^{\prime}/\,$  Manoj D. Nene

**Thesis submitted to the faculty of the Graduate School of The New Jersey Institute of Technology in partial fulfillment of the requirements for the degree of Master of Science in Engineering 1991** 

# APPROVAL SHEET

Title of Thesis: Bio-Mechanics of the Hip-Joint and the Engineering considerations in the treatment of Unstable Intertrochanteric fractures

Name of Candidate: Manoj D. Nene Master of Science, 1991

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# DEDICATION

I would like to dedicate this thesis to my parents and my family members whose support and encouragement helped me in furthering my education, and to my beloved wife who has been a constant companion and a source of inspiration through testing times.

# ACKNOWLEDGEMENT

I would like to take this opportunity to thank my advisor Dr. Raj Sodhi for providing me with all the help and guidance necessary to sucessfully complete my thesis. I would also like to sincerely thank Mr. Katkuri Reddy, M. E. Dept. for spending his invaluable time in assisting on the CAD portion of the thesis work. Last but not the least I would like to thank Dr. David Kristol, Chairman of the Bio-Medical Engineering program for his patience and help in completing the Masters program.

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# CHAPTER I

## **INTRODUCTION**

## **1.1 Background:**

Internal fixation of intertrochanteric hip fractures with a sliding hip screw or nail has proven to be a superior method of fixation as compared to the use of rigid nail-plate devices.

The sliding device allows controlled impaction of bone fragments to a. stable configuration, restoring the medial weight-bearing buttress of bone. This allows load transmission across the fracture site and makes early ambulation with full weight bearing possible. The sliding action also minimizes the possibility of nail penetration and cut out.

## 1.2 **History:**

Galilei along with others like Ward<sup>42</sup>, Wyman<sup>46</sup>, Haughton<sup>19</sup>, Pauwels have all discussed the load bearing capacity of bones. They all felt that there is a relation between the design and function of the bone. The design of the proximal femur, the head and the neck, and it's internal architecture has been the subject for mechanical analyses. The femoral head is not exactly spherical in shape but, slightly compressed in an approximately ventro-dorsal direction. The femur is both non-linear and non-homogenous in geometry. The femur has both a mixture





of isotropic and anisotropic properties. The femoral neck lies in a distal-lateral direction. It is like a long tube compressed in the ventro-dorsal direction. The neck changes shape during its entire length. A section through the neck is almost cylindrical at its junction with the head. The shape of the neck becomes elliptical in a distal lateral direction.

The cortical shell of the neck is as thin as paper at its head. As the shaft is approached the cortical bone increases its thickness gradually. In the superior part of the neck, the increase is small, but in the inferior part, the thickness increases considerably and is maximum where the major axis intersects the cortical bone. Hence, in a section through the major axis the cortical bone is strongest in the inferior part.

The hip-joint is a ball and socket type of joint composed of acetabulum and the femoral head as shown in Figure 1. The cartilage covering the femoral head has non-uniform thickness, which results in different elastic properties in different regions of the femoral head. These different mechanical properties from point to point affect the transmission of stresses from the acetabulum through the femoral head to the femoral neck. The distribution of stresses on the femoral head is very complex.

To understand the design of the upper femur and its relationships to the forces acting on the bone, the angle formed by the neck with the femoral shaft must be known.





Fig.2 Geometrical skeleton of the femur illustrating functional axes, applied angles and planes.

The angle formed by the neck of the femur and the shaft, the cervicodiaphyseal angle is defined as the angle formed between the cervical axis OHC and the ideal axis AOK (Fig.2). On an average this angle is about 54°.

The cervico-diaphyseal angle can also be defined as the angle formed by the cervical axis OHC and the proximal longitudinal axis of the femoral shaft OD.

A plane through the ideal axis and the cervical axis AOKC is called the antetorsion or the anteversion plane (Fig. 2). The mobility in the hip-joint and the force relationships are functions of the cervico-diaphyseal and ante-torsion angles.

The variations of the cervico-diaphyseal angle, the antetorsion angle and the principal plane under normal and pathological conditions have been the subject of different mechanical interpretations. Investigators in this field feel that changes can take place in the design of the bone in order to permit yeilding to existing mechanical stresses.

 $Milch<sup>28</sup>$  maintained that the direction of the resulting force can be determined by the analysis of the internal structure. Gluckmann<sup>17</sup> believed that the tensile stress provokes the formation of bone and affects the architecture. Pauwels on the basis of theoretical analysis and experiments believed that the trabecular system is built up in order to achieve a framework with minimum of material.

Bone apposition and resorption are caused by the magnitude of stress and due to remodeling, the lamellae will have the same direction as though they were stress lines. Stress on the epiphyseal cartilage according to Pauwels may affect the



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Fig. 3 Intertrochanteric Fracture- Four Sections

bone growth. Tensile stress on the epiphyseal cartilage would simulate growth in length, while thickness is determined by compressive stress.

Kummer felt that the skeleton is built up with a minimum of material in order to resist the required stress. The upper femur can be regarded as a crane, but he disapproved photo-elastic tests on the models for analysis of the trabecular system, as the magnitude and direction of forces acting on the hip joint are unknown.

Symth<sup>39</sup> inquired about a quantitative method for measuring forces in the hip-joint, as the muscular force is difficult to evaluate. He believed that bones can be formed to resist stress in the best possible way.  $Garden^{15}$  believed that the internal architecture of the femur cannot be determined by mechanical principles, but that the structure arises through rotation and expansion from the shaft of the femur.

## 1.3 **Definition of Intertrochanteric Fracture**

An unstable intertrochanteric fracture of the femur is shown in Fig. 3. An unstable intertrochanteric fracture lacks continuity of the bone cortex, on the opposing surfaces of the proximal and digital fragments. This cortical defect is due to either comminution on the medial aspect of the neck (calcar region), or a large and seperate posterior trochanteric fragment. Sometimes combination of the two is present. The instability is generally unrecognized, and anatomical reduction does not restore stability.

The internal fixation of intertrochanteric hip fractures with a sliding hip screw or a nail has proven to be a superior method of fixation. The sliding device allows a more uniform load distribution at the fracture site, which makes early ambulation and full weight bearing possible.

### 1.4 **Materials of Construction of Sliding Devices**

Failures of many of these nails initiated study of design and the construction of a nail, which could be trusted to withstand the stresses, normally encountered in the post-operative period, of the typical elderly patient, with an intertrochanteric fracture.

Secondary consideration in the design of a stronger nail plate was the possibility, that many elderly patients would safely be encouraged to bear weight on the fractured hip, thereby acquiring the obvious advantages of bi-pedal gait. In intertrochanteric fractures however, the problem is more complex because of osteoporosis, comminution and the consequent difficulty in securing truly stong fixation.

From Table I, it can be seen that various types of nails such as Smith-Petersen, McLaughlin, Jewett type, Holt, V-nail plate were used for analyses. **The**  metals that were primarily used were S.S. **301, S.S. 316, A-286, AISI 316,** CoCr alloys, SMo S.S., Titanium and Vitallium. **The** angle of the nails used varied from 125° to 155°. The maximum load bearing capacity was found to be in a **Holt-**Vitallium 130° type of nail which was angle mounted at 3/4" above the edge **of**  the plate. Most of these nails were mounted either  $1/2$ ",  $3/4$ ",  $7/8$ ",  $1$ " or  $1\ 1/8$ " above the mount. The common failure among these nails was found to be plate bending at the top screw hole, at the nail plate junction or at the mount.

### 1.5 **Previous Fixation Methods/Techniques**

Functional recovery can be achieved by both operative and non-operative treatment of intertrochanteric fractures. The operative treatment is preferred because, following adequate internal fixation of these fractures, the patient is spared the hazards and expense of prolonged recumbency.

There have been various suggestions by authors concerning the treatment of comminuted unstable intertrochanteric fractures. Evans<sup>11</sup> advocated fixation in the position of varus deformity, while Dimon and  $H$ ughston<sup>10</sup> advised medial displacement of the distal fragment. Boyd and Anderson' suggested placing a buttress plate laterally to prevent varus displacement, but accepted that medial displacement of the distal fragment, at the time of the operation is often the only way of achieving stability, in these comminuted unstable fractures. All authors have emphasized the importance of creating bony stability at operation.

Stable intertrochanteric fractures are satisfactorily treated with rigid internal fixation devices, but recognition of the type of fracture which will be satisfactorily stabilized is not always possible as pre-operative radiographs do not reveal the extent of communition that is present.

Surgeons use guide pins<sup>9</sup> to help insert the nail. Using the guide pin helps



Fig. 4 Method of Guide Pin Placement

in ensuring proper placement of the screw and prevents destruction of bone because of repeated insertions. The guide pin also establishes the exact length of the nail and permits placing the nail at the same angle to the shaft, as the fixed angle of the nail plate.

Treatment of intertrochanteric femoral fractures is achieved through the use of Sliding Screw Plates, while treatment of trochanteric fractures is achieved using Compression Screws, Nail plates.

## 1.6 **Modern Fixation Devices**

In recent years the development of the hip fixation devices has led manufacturers to use superior quality materials, to produce nails and sliding devices. Materials like Vitallium, alloys of Titanium, Molybdenum, Chromium, are used which have strong mechanical properties and are easy to manufacture.

Dow Corning utilizes 316 LVM S. S. ASTM F-55 as its material of construction for all its fixation devices. DePuy uses its own DePuy certified S. S. as its material of construction. The sizes for tube length for both the 135° and the 150° compression screw manufactured by Dow Corning varies from 38 mm to 64 mm, while the plate length varies from 102 mm to 152 mm for the Dow screw. The Synthes screw has two tube lengths, 25mm and 38mm, while the plate length varies from 46mm to 270mm. Similarly in case of DePuy the plate length comes in varying sizes from 70 to 260mm for the compression hip screw. The number of holes vary from 2 to 12 for the three screws.

The nail length for a 135° or 150° Jewett nail manufactured by DePuy varies from 50 mm to 305mm, while the plate length varies from 89 mm to 146mm. The number of holes vary from 3 to 6.

#### 1.7 **Previous Finite Element Studies**

The Finite Element Method(FEM) is an advanced computer technique of structural stress analysis developed in Engineering Mechanics, introduced to Orthopedic Bio-Mechanics to evaluate stresses in human bones. Since then, this method has been applied for stress analysis of bones, bone-prosthesis structures, fracture fixation devices and various kinds of tissues other than bones.

FEM analyses are based on theories of continuum mechanics. The continuum materials involved in the analysis of bones are the cortical (or compact) bone, and the trabecular (or spongy) bone. On a macroscopic level the trabecular bone is noncontinuous, and hence considered a structure rather than a material. But, in quasi-static loading, both cortical and trabecular bone behave linear elastic by approximation (although they are considered anisotropic and non-homogeneous). Their elastic properties depend on age, species and mineral content.

The cortical shafts of the long bones, have irregular beam-like geometries. Their metaphysical and epiphyseal ends are irregular in shape. Bone loading is dynamic due to muscle and gravitational forces, **and** little is known about its characteristics.





Finite element analysis is presently being used to investigate the stressrelated architecture of bone, and bone remodeling processes, to test and to optimize, artificial joint designs and fracture fixation devices, and to study the mechanical behavior of tissues, such as articular cartilage and intervertebral discs.

The femur is the most frequently analyzed bone due to its involvement in orthopedic treatments, such as prosthetic replacement of fracture fixation. Early FEM for stress analysis of the femur by Brekelmans<sup>2</sup> (fig. 5) and Rybicki<sup>36</sup> were aimed at demonstrating the possibilities of the FEM. They both applied 2-D plane stress elements of uniform thickness, by varying the Young's moduli of the elements. Rybicki only analysed the proximal part of the bone, accounting for non-uniform thickness. The results were comparable to a 2-D beam model analysis, but only agreeable in the diaphyseal part. A similar model was used by Wood<sup>45</sup> et al.

The early 3-D FEM models of the femur demonstrated the problems associated with data manipulation, interpretation and representation. Some models contained a high degree of sophistication, such as realistic non-homogeneity of trabecular bone. The data generated for the shaft of the femur, compared favorably among different mathematical models.

The 3-D model developed by Scholten is a refined one, with a high mesh density (approximately 10,000 degrees of freedom). Valliappan's <sup>45</sup> model consisted of higher order elements. Valliappan et al. roughly compared FEM results with those of stress-coat experiments, revealing good agreement in a relative sense.

Rohlmann<sup>34</sup> et al. achieved the same conclusion, based on a comparison between 3-D FEM and strain-gage experimental results, from paired femoral bones.

Huiskes et al.<sup>23</sup> showed through detailed experimental and theoretical analyses on bilateral bones, that the femoral shaft can be modeled refined, when the cortical bone is assumed to be transversely isotropic.

A 2-D Finite element model of the femoral head was developed by Brown and Ferguson'. It included nonhomogeneous elastic properties of trabecular bone. The study was aimed at investigating the influences of trabecular bone nonhomogeneity and of geometrical varus-valgus alterations on the stress distribution. Brown et al.4, later extended the model to the proximal femur, where anisotropy was included and mechanics of the femoral head in presence of avascular necrosis were studied.

Brown et al.<sup>5</sup>, developed a 2-D FEM model of the proximal femur, to study the collapse phenomenon of trabecular bone in aseptic necrosis including non-linear elasto-plastic material behavior.

Similarly other researchers subjected their studies towards bone growth and remodeling. Hayes<sup>20</sup> et al., attempted to correlate the trabecular bone architecture of the human patella, and its stress distribution for the quantification of Wolff's hypothesis. They found that high Von Mises effective stress, correlates with regions of high trabecular density, and that the trabecular structure aligns itself with principal stress orientations. They also demonstrated that anisotropy of trabecular bone hardly affects the stress distribution, if its nonhomogeneity is accounted for.

Pugh<sup>32</sup> et al., studied stresses in the trabeculae using simple plate elements. The aim was to correlate local bone loading with trabecular failure. A 2-D FEM model was proposed by Williams and Lewis<sup>43</sup>, to predict the elastic constants of trabecular bone as a continuum material, from the non-continuous trabecular structure and properties.

Stress related remodeling of bone, investigated by Hassler et al.<sup>18</sup>, evaluated stress predictions in a piece of rabbit skull, loaded locally by an apparatus applying 2D and 3D models. The stress distribution was evaluated at particular time intervals.

Chand et al.<sup>7</sup>, used a 2-D FEM model and an iterative algorithm to investigate the unbonded elastic contact problem between femur and tibia in the knee joint. Results were comparable to those of 2-D and 3-D photoelastic analyses. A simpler 2-D model of both the tibia-femoral, and the femur-patellar complex was reported by Valenta et al.<sup>40</sup>, in which contact areas were presumed. Hayes et al.<sup>20</sup>, presented an axisymmetric FEM analyses (non-axisymetric loading) of the upper tibia. Hayes was effective in demonstrating the load transmission in the upper tibia and it's relation to the bone structure.

A 3-D FEM model of the lower femur and upper tibia was reported by Roehrle et al.<sup>33</sup>, Roehrle did not model the whole tibia. Piziali<sup>30</sup> et al., used the FEM to solve Saint Venant's warping function for torsion, in a cross-section of this bone. *Fracture Fixation Devices:* 

In recent years interest has been focussed on the fracture fixation devices, because the use of fracture fixation devices may weaken the bone through disuse osteoporosis or bone resorption, particularly due to the application of bone screws and pins. There have been suggestions that bone-remodeling and bone-resorption phenomenon may be initiated by micro-fractures, which would be of importance in implant design and fixation. Fracture mechanics of the bone have not been studied with the FEM, although considerable advances in this area were reported for other materials in engineering mechanics.

The fracture fixation devices are used extensively in orthopedic and general surgery. Their mechanical characteristics are important due to strength requirements, and the influence of their fixation rigidity on the fracture healing process. Use of the FEM in an analysis of a bone-fracture plate complex was first reported by Rybicki<sup>35</sup>et al. Subsequently Rybicki and Simonen<sup>36</sup> analysed a 2-D FEM model, of an oblique fracture stabilized with bone plates. Stresses at the fracture site were evaluated, for varying circumstances, such as pretension in plate, bone screw orientation and bone loading.

Simon et al.<sup>38</sup>, performed an extensive comparison of beam, 2-D and 3-D FEM models, and experimental findings with respect to the bone plate. All three models gave comparable results, but more detailed information was obtained from from the 3-D model at a specific location. The FEM beam model in the study was subsequently studied by Woo et al.<sup>50</sup>, to study bone remodeling, comparing FEM results to the remodeling findings in animal experiments. Carter<sup>6</sup> et al., studied bone remodeling in particular by comparing stress fields, with in-vivo bone resorption phenomena. The FEM was applied for local cross-section, to evaluate shear-stresses in torsional loading.

Using 3-D FEM beam elements Chao and  $An^8$ , evaluated frame rigidity in several configurations out of different materials, in combination with experimental analyses. The sites, at which the pins of these frames are connected to bone are usually heavily stressed, making bone liable to pressure necrosis.

Fracture fixation by nailing received attention where FEM analysis was concerned. A 3-D non-linear FEM model to study trochanteric femoral fractures was presented by Ghassemi<sup>17</sup> et al. Valenta<sup>44</sup> et al., previously studied a linear 2-D FEM model. Due to the large variety of fracture types, it is doubtful whether an anatomic (geometrically refined) 3-D model is helpful in analyzing these structures, especially when non-linear effects are taken into account. Hence, it would be realistic to aim for general information on a relative basis, in the case of fracture fixation FEM modeling.

## 1.8 **OBJECTIVE:**

This work examines the variables involved, in the treatment of unstable intertrochanteric fractures of the hip. The study will identify the variables involved

in the placement of the lag screw, and in the design of the screw plate. The study shall also investigate the biomechanics of the hip joint to determine the transmission of forces through the femoral neck, identifying the variables involved like the plate angle, and the eccentricity of the screw-plate. A mathematical model is developed to obtain the relationships between these variables, and study the possibility of theoretically determining the optimal design, of the screw positioning and the plate geometry. A 3 -dimensional finite element model of the plate is also developed to study the stresses developed, and a comparison of stresses acting on the plates is done to determine an optimal design. Design modifications are suggested to allievate the stresses at the corners of the plates.

# CHAPTER II

# **Mechanics/ Stress Analysis of Intertrochanteric Fracture:**

## 2.1 **Mechanics of Intertrochanteric Fracture**

Proper use of a sliding screw or nail requires an understanding of the mechanics of the intertrochanteric fracture as well as the mechanics of the device used. The stability of the proximal femur depends primarily on the medial cortex. When a significant segment of the medial cortex is fractured, as in an unstable intertrochanteric fracture, the stability is lost, which allows the fracture to displace into varus. The integrity of the medial weight-bearing buttress of bone must be restored, before ambulation with full weight bearing is possible. The medial buttress can be reconstituted with osteotomies, or medial displacement, or by allowing impaction of fracture fragments so that this area resumes its function as a load-carrying structure. If this is not done and the patient is allowed to ambulate, the forces generated across the hip are so great that nail penetration, breakage, cut out and various deformities may occur.

## 2.2 **Mechanics of Sliding Fixation Devices**

The use of compression hip screws for the internal fixation of hip fractures has gained popularity in recent years, because of its ability to provide solid

bending fixation of the two major fracture fragments, while allowing physiological compression at the fracture site and minimizing the possibility of nail penetration or cut-out. The controversy over the use of a high or low angle plate in the placement of the screw remains unsolved. It is advantageous to have a low-angle nail because of its ease of insertion. Massie and others have asserted that as the angle of the nail plate approaches the normal weight-bearing axis of the hip, the bending moment on the nail decreases. This may result in greater ease of sliding of a compression hip screw, less potential for jamming, and better bone impaction at the fracture site.

To understand the mechanics of a sliding fixation device, one must first understand the forces that act on the device. The magnitude and direction of the force exerted across the hip joint are dictated by the body weight, and the muscles acting on the hip.

In 1935, Pauwels published studies on the forces about the hip applied at an angle of 60° to the horizontal plane, and concluded that they represent about three times the body weight, in a single-leg stance phase. These results were confirmed by others. Frankel<sup>12</sup> showed that after osteosynthesis of experimentally created femoral-neck fractures, the bone absorbs as much as 75 percent of the load applied to the femoral head. Applied load on the nail plate can therefore be assumed to be 25 percent of the resultant load, during single-leg stance phase for an average adult person. This load represents the minimum force applied to the



Fig. 6 Resultant force divided into two components, parallel and the other perpendicaular to the sliding axis of the screw.

screw in a patient who would be allowed to walk immediately after osteosynthesis.

The resultant force (Fig. 6) across the hip can be resolved further into components parallel and perpendicular to the screw axis. Only the perpendicular component creates a bending moment in the screw. The magnitude of the perpendicular force component applied to the screw is dependent on the divergence of the screw plate angle from the normal weight-bearing axis of the hip.

As the angle of the sliding axis of the fixation device neared the direction of the resultant force acting on the hip, the greater was the force exerted to slide the device. As the nail-plate angle of the fixation device digressed, from the direction of the resultant force acting on the hip, a weaker force was exerted parallel to the sliding axis. A large perpendicular force was undesirable, since it would act to bind or jam the sliding mechanism preventing fracture impaction.

To calculate the perpendicular load on the screw, we consider a 2000 newton force acting on the hip joint weighing 154 lbs., in the single-leg stance phase of gait. Since  $\text{Frankel}^{12}$  concluded that bone absorbs 75 percent of this load in the presence of a fracture-fixation device. The minimum force that will be exerted on the screw is 500 newtons (25 percent of 2000 newtons). When resolved into components parallel and perpendicular to the screw, the resultant perpendicular to the screw, the resultant perpendicular load component for a 130° nail plate is equal to

$$
B_0 = 500 \sin[159 - 130]^{\circ} = 242.4
$$
 newtons


 $Fig. 7$ Free Body Diagram of a Compression Hip Screw showing resultant force applied across the hip divided into perpendicular load( $B_o$ )and an axial load  $(A_o); b_1, b_2$ . perpendicular reaction forces and  $a_1$ ,  $a_2$ -resultant frictional forces.

Similarly the resultant perpendicular load component for a 150° nail plate is equal to

 $B_0 = 500 \sin[159 - 150]$ ° = 78.22 newtons

The force component parallel to the barrel was the component that produced sliding of the screw. When the parallel component exceeded the maximum static frictional force between the screw and the barrel, sliding was initiated. This maximum static frictional force was controlled by the magnitude of the perpendicular force component, and the actual coefficient of friction between the sliding surfaces.

Fig. 7 shows a free-body diagram. The force B<sub>o</sub> acting perpendicular to the screw applied over the distance  $L_n$  must be counteracted by the reaction forces b<sub>1</sub>, b<sub>2</sub> created between the screw shaft and the barrel acting over the distance  $L_b$ . Since the distance  $L_b$  was shorter than the distance  $L_n$ , the reaction forces created at the screw barrel interface were great. The parallel force  $A_0$  acting to slide the screw was counteracted by the frictional force between the screw shaft and the barrel  $a_1$ ,  $a_2$  as a result of the perpendicular load  $B_o$ .

As the nail-plate angle increased the ease of sliding increased in an exponential manner. Clinically, no control exists over the length of the screw extending from the barrel  $(L_n)$ , because the screw must be placed well into the femoral head to obtain maximum purchase of the proximal fragment. The amount that the screw is engaged in the barrel would then be controlled.

The sliding characteristics of any of these devices are determined by two parameters: the appparent coefficient of friction and the actual coefficient of friction. The actual coefficient of friction is simply defined as the ratio of the amount of force required to slide pieces of metal one over the other (force parallel to the surfaces) to the amount of force pushing over the two surfaces together (force perpendicular to the surfaces). This coefficient of friction is usually thought to be dependent on the material and the nature of the surfaces of those materials.

The apparent coefficient of friction is a property not only of the type of material and the surface finish but also of the geometric characteristics of the sliding hip nail. The apparent coefficient of friction is defined as the ratio of the force parallel to the screw barrel  $(A_0)$  that is required to initiate sliding when the tip of the screw is loaded with a force applied perpendicular to the barrel  $(B_0)$ . Here, the amount of force required to initiate sliding will depend on the length of the screw extending from the barrel  $(L_n)$  as well as the length of the screw in contact within the barrel  $(L_b)$ .

From the conditions of static equilibrium and the assumption that the actual coefficient of friction  $(\mu)$  is defined as the ratio of the tangential forces (a<sub>1</sub> and  $a_2$ ) to the normal forces ( $b_1$  and  $b_2$ ) at the contact points between the screw and barrel, the following expression for  $\mu$  is obtained:

$$
\mu = \frac{a_1}{b_1} = \frac{a_2}{b_2} \tag{2.1}
$$

$$
\mu = \frac{A_{\circ}/B_{\circ}}{1 + 2\frac{L_n}{L_b}}\tag{2.2}
$$

Therefore, the actual coefficient of friction between the sliding surfaces  $(\mu)$ is determined from the earlier equation while the apparent coefficient of friction  $(\mu_{\circ})$  is determined from its definition

$$
\mu_{\circ} = \frac{A_{\circ}}{B_{\circ}} \tag{2.3}
$$

where  $A<sub>o</sub>$  is the parallel load component and  $B<sub>o</sub>$  is the perpendicular load component at the proximal tip of the screw.

Tests have been carried out by previous researchers to examine the effect of screw-plate angle on the sliding characteristics and jamming potential of four commonly used S.S. and CoCrMo compression hip screws. The actual coefficient of sliding friction for these alloys was also measured in each device. The force on the screw required to overcome the static frictional force was also determined, representing 130-degree and 150-degree screw-plate angles. For the 130-degree plate this force was significantly higher<sup>29</sup> than that required for the 150-degree loading configuration. The actual coefficient of friction was found to be relatively constant for each material.

If the length of the screw extending from the barrel is very long as compared to the length engaged in the barrel, jamming occurs. Jamming results from gross surface distortion in an uneven and unpredictable manner between the two



Fig. 8 Load applied to initiate sliding

surfaces, and this distortion greatly increases the actual coefficient of friction, and prevents surface sliding. The composition of metal alloy also influences jamming.

Results<sup>29</sup> have shown that all 316L S.S. screws jammed when tested at the 130-degree loading configuration, with the screw extending 10.2cms from the end of the barrel. It was also found that none of the screws jammed at the 150-degree loading configuration. The maximum static frictional force that was required to initiate sliding for the 130-degree loading configuration was significantly higher than that measured for the 150-degree loading configuration.

From these tests<sup>29</sup> it was clear that two factors appear to control the ease of sliding and the potential for jamming. The first was the amount of contact force generated between the distal tip of the screw, and its surface of engagement within the barrel. As the screw was extended from the barrel, the contact forces within the barrel increases. The second factor influencing the potential for jamming is the composition of the metal alloy.

In an intertrochanteric fracture the choice of the screw angle  $(\beta)$  was an important consideration. In order for sliding to occur, the parallel load component  $(A<sub>o</sub>)$  applied to the tip of the screw must exceed the load  $(A)$  required to initiate sliding. So, the ratio  $A_o/A$  was a measure of the sliding capability of the device.

In Fig. 8 a load P was applied to the tip of the screw. Assuming this load to be directed at 158 degrees to the long axis of the femur and the plate, the components parallel and perpendicular to the screw axis are  $A_o = P$  cos (158°- $\beta$ )

and B<sub>o</sub> = P sin (158 ° -  $\beta$ ) respectively. The axial load A to initiate sliding, was found to be governed by the perpendicular component of the applied load, **Bo ,** the actual coefficient of fricition  $(\mu)$ , and the length of the screw extending from the barrel  $(L_n)$ . Maximizing the sliding capability of the sliding hip screw, therefore, required that the ratio of  $A_o/A$  be as large as possible.

It is then evident from the discussion that if the length of the screw extending from the barrel increased or the barrel length decreased, more resistance is required for sliding, and there is a substantial rise in the potential for jamming. The only way to reduce the risk of jamming is by engaging the screw deep into the barrel and thereby lengthening the lever arm  $(L_b)$ .

#### 2.3 **Mathematical Analysis of Stress in the Human Femur**

In order to calculate the stresses in the human femur, muscle forces acting at the femoral head have to be taken into account alongwith the body weight. By adding inertial forces to the body, there is an increase in the body weight by a multiplicative factor which also tends to increase the stresses acting on the femur by the same factor.

The muscles considered for the stress analysis in the femoral head region are the hip abductors and the tensor fasciae latae. These muscles are chosen because equilibrium requirements provide a range of values for their muscle forces. Other muscle groups such as ilio-psoas, the short hip rotators, the hip abductors and the gluteus maximus are active, but it is more difficult to evaluate values for these muscle forces.

The major muscle groups of concern in the one-legged stance are the abductor group and the ilio-tibial tract. The latter is only in tension, above the greater trochanter, when the pelvis is in an extreme sagging position. The gluteus minimum and the gluteus medius muscles exert 3/4 of the total abduction force M and are inserted into the greater trochanter. The gluteus maximus and the tensor fascia latae are inserted into the ilio-tibial tract below the greater trochanter. These two muscles supply 1/4th of the abduction force. Thereby the force T in the ilio-tibial tract is unlikely to be greater than 0.25M.

The combined effect of force in the gluteus maximus, tensor fascia latae and ilio-tibial tract is an inward force on the lateral boundary of the greater trochanter, and is assumed to be distributed on the distal lateral trochanter surface. The head load was assumed to be distributed over a 60° arc on the femoral head.

The values for forces and the angles at which they act obtained by McLeish and Charnley for a body weight of 158 lbs.are

 $M=1061N$ , J=1620N, T=172N,  $\phi = 24.4^{\circ}$ ,  $\theta = 29.5^{\circ}$ 

Similarly Paul and Morrison have examined the mechanics of walking and estimated the muscle and joint forces acting on the femur. In the one-legged stance phase between the time interval from heel-strike through foot flat these results were evaluated. There are five stages in the walking cycle where the various muscle and joint forces peak almost simultaneously. These occur at 2%, 13%, 19%, 50% and

63%. The magnitude of forces as determined by Paul and Morrison for these five instances are listed in Table III.

The stress analysis on the femoral shaft in the past has been analyzed using the beam theory. An axial load of 165 lbs. was applied to the head of the femur, reacted by a force of equal magnitude and opposite direction at the distal end. For a man weighing 200 lbs., the axial load corresponds to the body weight less the weight of one leg. Results have shown that a maximum tensile stress in the shaft of the femur was 11.5MPa.

To maintain the one-legged stance the action of the hip abductor muscles have to be taken into consideration. The resultant force acting on the greater trochanter would create a moment to prevent rotation of the body about the hip joint. This force was estimated to be around 358 lbs. The addition of this force increases the axial compression in the femoral neck, giving a joint load of 525 lbs. at the head of the femur.

When the abductor muscle force was included by researchers the maximum tension in the femoral shaft was found to be 45.7MPa. This meant that the stress was increased four times the normal stress when the abductor muscle force was considered.

# CHAPTER III

# **Biomechanics and Forces acting on the Hip-Joint**

# 3.1 **Biomechanics of the Hip:**

Biomechanics is a basic science of orthopaedics utilizing the principles of Engineering Science in understanding mechanical dearrangements of the body. Biomechanics deals with motions and forces, and the interrelationships between them. Body movement is brought about by proper applications of these forces. These forces also have internal effects which produce a state of strain. The amount of strain and deformation the body will undergo depends upon its particular mechanical characteristics.

Biomechanics is sub-divided into four groups. The first group is involved with the mechanical properties of the tissue, concerned with basic tissues of cartilage, cancelous bone, cortical bone, etc. The study of substructure like the upper end of femur, hip joint and acetabulum forms the second domain. Kinematics the third sub-group deals with description of the motion of the whole joint, or of the motion on or about the joint surface. The fourth group deals with loading of the structure in use.

#### 3.2 **Forces acting on the Hip Joint**

The hip joint is surrounded by large muscles and strong ligaments. The



Fig. 9 Force Diagram of the Normal Femur

muscles, and to a certain extent, the ligaments affect and complicate the calculations of the forces which act on the head of the femur. Understanding the biomechanics of the hip joint has been rendered difficult because of lack of knowledge of the magnitude and direction of forces acting on the hip joint. Meyer suggested that the joint cartilage be subjected to a pressure which is determined by gravity and muscular force. Fick, Milch<sup>28</sup> and Debrunner pointed out the importance of muscular action on the hip-joint.

Many previous attempts have been made to calculate the resultant force acting on the head of the femur. Henke, Thomsen and Kuntscher suggested that both muscular and gravitational forces have to be considered, when calculating the forces acting on the hip-joint.

Pauwels felt that the center of gravity lies eccentrically in relation to the longitudinal axes of the bones and this may provoke heavy bending moments. Koch<sup>26</sup> calculated the dynamic load twice the value than that of the static load. In gait the static load on the head of the femur is about 80 percent of the body weight and the forces acting against the head of the femur will be 1.6 times the body weight. Koch pointed out, that the femur may act as a shock absorber due to flexion in the hip and the knee. Grunewald felt that due to muscle forces, the value of the force acting on the hip-joint may reach 900 lbs. Storck calculated the muscle force to be equal to twice the value of the body weight.

Pauwels on the basis of Fischer's works calculated the magnitude and

35

direction of the force acting on the head of the femur in a single-leg support, two-leg support and during the stance-phase in gait. The muscle forces in the horizontal plane were found to be negligible in both the single-leg stance and the two-leg support phase. While walking, a dynamic component is added in the horizontal plane. The dynamic component in the frontal plane is predominant. Pauwels believed that insignificant muscular forces act when standing on two legs, and the vertical force acting down is equal to one-third of the body weight.

In a single leg support, the muscular forces affect the magnitude and direction of the resultant force. The center of gravity for the superimposed body weight was assumed to be 109 mm. from the center of the head, and the lever of the abductor muscle was estimated to be at 40 mm. The force acting on the head of the femur will then be about three times the value of the total body weight. If consideration is given to the dynamic forces during the stance phase the forces will be about four and a half times the body weight. When using a walking stick, the vertical force can be reduced to approximately 1.7 times the body weight.

Other researchers Cabot and Peralba, Knese, Muller, Hackenbroch, Williams and Lisner, Hochman and Hauge found out that the force or load acting on a single-leg or in gait varied between four and six times the body weight.

The resultant forces will not be absolutely vertical because of the muscles. So far all the calculations have been made for the frontal plane. Storck felt that the force in the standing position on one leg forms an angle of 15° with the

vertical plane. Pauwels believed that standing on two legs results in a vertical force, because the muscular components are insignificant. The force in the frontal plane forms an angle of 16° with the vertical line. Pauwels also found that in the horizontal plane it forms a dorsally open angle with the frontal plane, of about 30° in the beginning of the stance-phase and at the end of the phase it reaches a minimum angle of 2° with the frontal plane.

Inman<sup>24</sup> thought that the direction of the force in one-leg support is constant, irrespective of the position of the pelvis. The force direction forms an angle of 10° - 15° with the vertical line in the frontal plane which corresponds to the direction of the medial trabecular system. The epiphyseal line runs perpendicular to the medial lamellae. As the resultant force seems to follow these trabeculae, no consequent shearing force will arise on the epiphyseal cartilage in the frontal plane.

The magnitude of the pressure arising on the head of the femur depends on the size of the contact surface. It is difficult to conclude exactly, since one cannot be certain that the center of the contact surface coincides with the point of force application. Fick thought that the medial upper portion of the head of the femur is subjected to the greatest pressure since its lateral position lies outside the acetabulum. Buchet and Castaing pointed out that the anterior part of the femoral head is of greater importance to the mechanics of the hip-joint. The resultant force runs along the longitudinal axis of the neck and forces the head of the femur upwards, inwards and forwards in the standing postion.



Fig:10 BEAM ANALYSIS OF PLATE

# **CHAPTER IV**

#### **SYSTEM MODEL**

To calculate the stresses acting on the plate it is very essential to setup a Mathematical model based on the assumption that it is a solid beam having an uniform thickness. The plate can then be analysed by beam analysis method. The dimensions for the plate were obtained from the Manufacturers handbook. To compare the 135° and a 150° plate we first need to setup standard equations for the plate, such that it would give us approximate values of stresses, acting at different points along the entire length of the plate.

# **Nomenclature**

- $\theta_1$  = Angle of plate (135° or 150°)
- $\theta_2$  = Angle at which force P acts = 24.4°
- $l_1 =$  length of the plate
- $l_b =$  length of the barrel
- $P =$  Load or force transmitted by bone
- $E =$  Modulus of Elasticity
	- $= 200 \times 10^3$  MPa for 316L S. S.
	- $= 240 \times 10^3$  MPa for Co Cr Mo S
	- $= 100 \times 10^3$  MPa for Ti (ASTM-F67)

$$
M =
$$
Bending Moment

- $y = deflection$
- $I =$  moment of inertia
- $Z =$  section modulus

$$
\sigma = \tfrac{M}{Z}
$$

### Assumptions:

- [1] The plate is assumed to have an uniform cross-section.
- [2] Previous results have proved that the plate bends at the first hole hence all forces are assumed to be concentrated at the first hole and none are transmitted beyond the first hole.
- [3] No moments are assumed at the four holes.
- [4] The holes for the bolts are assumed to be equidistant.

$$
\sum X = X_1 + X_2 + X_3 + X_4 - P \cos \theta_2 = 0 \tag{4.1}
$$

$$
\sum Y = R_1 + R_2 + R_3 + R_4 - P \sin \theta_2 = 0 \qquad (4.2)
$$

$$
\sum M = R_2 l + R_3 2 l + R_4 3 l - P \sin \theta_2 (l_1 + l_b \cos \theta_1) - P \cos \theta_2 (l_1 + l_b \cos \theta_1) = 0 \quad (4.3)
$$

$$
\sum M_z(x) = EI \frac{d^2 y}{dx^2}
$$
  
=  $R_1 x + R_2(x - l) + R_3(x - 2l) + R_4(x - 3l) + (X_1 + X_2 + X_3 + X_4)(x - l_1) \tan \theta_1$ 

Integrating once we get,

$$
EI\frac{dy}{dx} = R_1\frac{x^2}{2} + C_1 + R_2\frac{(x-l)^2}{2} + R_3\frac{(x-2l)^2}{2} + R_4\frac{(x-3l)^2}{2}
$$

$$
+(X_1+X_2+X_3+X_4)\frac{(x-l_1)^2}{2}\tan\theta_1
$$

Integrating further

$$
EIy = R_1 \frac{x^3}{6} + C_1 x + C_2 + R_2 \frac{(x-l)^3}{6} + R_3 \frac{(x-2l)^3}{6} + R_4 \frac{(x-3l)^3}{6}
$$

$$
+(X_1+X_2+X_3+X_4)\frac{(x-l_1)^3}{6}\tan\theta_1
$$

We have the following unknown variables

$$
R_1
$$
,  $R_2$ ,  $R_3$ ,  $R_4$ ,  $X_1$ ,  $X_2$ ,  $X_3$ ,  $X_4$ ,  $C_1$ ,  $C_2$ 

 $X_1 < X_2 < X_3 < X_4$ . The shearing force applied to the plate at each hole can be calculated since each is a function of  $X_4$  in terms of a constant k. k is calculated by the formula

$$
k=\frac{n-n}{n}
$$

where n=Total no. of screws

n'=Total no. of screws in the rows between the row being checked in tension and external load.

To find displacement at  $x=0$ ,  $x=l$ ,  $x=2l$  and  $x=3l$ 

$$
\delta_{x=0}=0
$$

 $\delta_{x=1}=0$ 

$$
\delta_{x=2l} = 0
$$

$$
\delta_{x=3l} = 0
$$

Substituting  $X_1 = k_1.X_4$ ,  $X_2 = k_2.X_4$ ,  $X_3 = k_3.X_4$  where  $(k_1 = \frac{1}{4}, k_2 = \frac{1}{2}, k_3 =$  $\frac{3}{4}$ ) and the conditions for displacement in equation for EIy we get,

$$
\delta_{x=0}=0=C_2\tag{4.4}
$$

$$
\delta_{x=l} = 0 = R_1 \frac{l^3}{6} + C_1 l \tag{4.5}
$$

$$
\delta_{x=2l} = 0 = R_1 \frac{(2l)^3}{6} + C_1 2l + R_2 \frac{l^3}{6}
$$
 (4.6)

$$
\delta_{x=3l} = 0 = R_1 \frac{(3l)^3}{6} + C_1 3l + R_2 \frac{(2l)^3}{6} + R_3 \frac{l^3}{6}
$$
 (4.7)

We have 7 unknowns and 7 equations, solving them we can get values for all unknown parameters.

For bending stresses we know that

$$
\frac{M}{I}=\frac{\sigma}{y}=\frac{E}{R}
$$

but

$$
\frac{I}{y} = Z = section \quad modulus
$$

Therefore,

$$
\sigma=\frac{M}{Z}
$$

For a beam with uniform cross-section

$$
I=\frac{bh^3}{12}
$$

and

$$
Z=\frac{bh^2}{6}
$$

Therefore,

$$
\sigma_{x=l_1}=f(P,\theta_1,\theta_2,......)
$$

We also know that  $\sigma_{real} = \sigma_{calc.} \times k$ 

where k=stress concentration factor found from tables.

Solving the equations simultaneously we have the following values:

 $X_1 = 0.25X_4$ ,  $X_2 = 0.50X_4$ ,  $X_3 = 0.75X_4$  $\sin \theta_2 = 0.413$ ,  $\cos \theta_2 = 0.9106$  &  $l_b = 38mm$ 

For a  $135^{\circ}$  plate

$$
\cos \theta_1 = 0.707
$$
  
\n
$$
X_4 = 0.364P
$$
  
\n
$$
C_1 = -R_1 \times \frac{l^2}{6}
$$
  
\n
$$
R_1 = \frac{P}{5.l_1 + 134.35} \times 0.084l_1 - 68.88
$$
  
\n
$$
R_2 = -6.R_1
$$
  
\n
$$
R_3 = 4.R_1
$$
  
\n
$$
R_4 = R_1 + 0.413P
$$
  
\n
$$
l = l_1 + 26.87
$$

Similarly using the same values for  $X_1, X_2, X_3, \theta_2$  and  $l_b$  for a 150° plate we get the value of  $R_1$ 

$$
R_1 = \frac{P}{5.l_1 + 134.35} \times [0.094 l_1 + 10.575]
$$

Knowing the values of the variables like  $P$  and  $l_1$  we can find the value of the unknowns like  $R_1$ ,  $R_2$ ,  $R_3$ ,  $R_4$ ,  $X_4$ ,  $C_1$ . Substituting these unknown values in the formula for moments at different lengths we get

$$
M_x = 0 \text{ for } 0 < x < l
$$
\n
$$
M_x = R_1.x + R_2(x - l) \text{ for } l < x < 2l
$$
\n
$$
M_x = R_1.x + R_2(x - l) + R_3(x - 2l) \text{ for } 2l < x < 3l
$$
\n
$$
M_x = R_1.x + R_2(x - l) + R_3(x - 2l) + R_4(x - 3l) \text{ for } 3l < x < l_1 - 3l
$$

Using the moment equations listed above for various values of x we get values of moment for P = 250 N and plate angle =  $135^{\circ}$  at x = 15 mm, 30 mm, 50 mm the values of  $M_x$  are -13,274 N-mm, 4852.63 N-mm and -75,243.66 N-mm.

To calculate stress we use the formula

$$
\sigma_{\bm{x}} = \frac{M_{\bm{x}}}{Z}
$$

The corresponding values of stress for  $b = 18$ mm,  $h = 10$  mm are -44.24N/mm<sup>2</sup>, 16.175 N/mm<sup>2</sup> and -250.81 N/mm<sup>2</sup>.

Similarly for a 150° plate the stresses for similar values of x are found to be 29.103  $N/mm^2$ , -10.88  $N/mm^2$  and -255.05  $N/mm^2$ .

# **Summary.**

From the above discussion it can be concluded that a mathematical model (from the given set of equations) is developed for the plate. Stresses at various cross-sections can be found using the mathematical model. Using stress charts we are able to calculate real value of stress. These values when plotted on a graph helps us to compare the behavior of the two plates.

# **CHAPTER V**

# **Computer Aided Design and Finite Element Modeling Introduction:**

Computer Aided Design (CAD) is used to graphically simulate a design problem. There are various software packages available like Autocad, Versacad, etc. Software packages like IDEAS (Geomod) is used to create an object model before an analysis is done on the two- dimensional or three-dimensional model to calculate stresses, displacement, etc.

# 5.1 **Basic Classification of CAD System**

Generally, any CAD system can be reviewed as a combination of two major functional components, mainly Design/Modeling and analysis.

In the Design/Modeling components, the system can be designed and modeled with basic data available to the designer. Here, with help of extensive menus the designer can develop the required system on the screen. Depending on the application, the user can also use the optimization software and 2-D or 3-D modeling system to develop it.

The second component of any CAD system is the analysis module. **Depending** on the CAD software used, and the area of application, the user can have different analysis modules such as a dynamic analysis module, finite element analysis module, etc. Here, the system which is designed and modeled by designer is put under various tests through analysis to check the design behavior. In some of the software, this component is optional and the users have an option to choose from various analysis software packages available on the market. In such cases the user should be cautious in checking the compatibility of the analysis module with modeling module.

## **5.2 Classification of CAD based on Dimension**

All CAD software can be broadly classified into the three categories, based upon the dimension it handles, viz.

- *[i] 2-D, Two dimensional:* CAD software treats the fiat object. These are generally called drafting software.
- *[ii] 2 1/2-D, Two and one-half dimensional:This* type of software is just an extension of 2-D software, i.e. it can handle three dimensional objects without side details.
- *[iii] 8-D. Three dimensional:* Treats 3-D objects with more complex geometries. Most of these software packages are capable of computing physical properties like mass, volume, inertia etc.

# **5.3 Classification based on Computer Hardware System:**

CAD software can also be classified based on the computer system on which it runs. The classification of computer systems is based on data processing approach, speed, accessible memory and cost. Both speed and memory depend mostly on word length, the number of bits a computer can handle at a time, that is 16 bit, 32 bit, etc. The main factors which dominate the processing speed and

amount of main memory that can be acessed are internal word length and external word length.

All CAD systems can be classified into three categories.

- *[a] PC based CAD system:* Most of the 2-D modelers can easily be run today on PC's without any extra hardware. Although many 3-D modelers running on PCs are as sophisticated as those available for large computers, wireframe/ surface modelers are a good fit for the PCs. This is true because they do not require as extensive computing-power of a computer, as is required by a solid modeler. Indeed, with a 30386 microprocessor based PC, wireframe/surface modeling can be almost as interactive as 2-D drafting. Most of the 3-D solid modeler perform functions such as shading to make a model appear realistic, section analysis for mass and inertia properties. These require intensive computation and time consuming operations, hence require increased power of PCs.
- *[b] Workstation based CAD System:* The popularity of Workstation based CAD systems is increasing day by day due to their powerful graphic capability and large memory storage. Workstations consist of three basic components, a primary processor and associated memory, a graphics display system and software. Networking ability is another element which is often found in Workstations.

Workstations typically place an emphasis on graphics display and manipulation, since this is an effective method of off-loading the host. The features of *a*  display system are directly related to the power of a display driver and not to

the characteristics of the terminal screen itself. Functions such as colorfill, line, arc generation and rotation are controlled by this display processor and associated with hardware.

[c] *Mainframe based CAD System:* The word mainframe is used to denote a large central processing unit or centralized computer system that can support more than one workstation and peripheral devices and can drive printers, tape drives, etc. Memory is important since mainframes are used in data-intensive tasks.

#### **5.4 Classification of CAD System based on Application:**

Major applications include CAD for Mechanical Engineering (MCAE), CAD for Electronics Engineering (EGAD), Petroleum exploration and mapping, Computer Aided Software Engineering (CASE), Bio-Medical Engineering Systems and Architecture, Engineering and Construction (AEC).

#### **5.5 Classification of CAD System based on Operating Systems:**

A CAD system uses different levels of software, these are an operating system, an application package and command language. An operating system is a computer program or collection of programs. The main function of an operating system is to access information and programs on auxiliary storage and other types of input or output devices. An operating system contains a file manager which keeps track of and handles information of files. The operating system takes the steps necessary to acquire the information and complete the task. It will do what is requested and places the result where instructed. In general, to control the

execution of other programs and to control the flow of data are the two basic functions of any operating system.

The two main operating systems in use today, are Disk Operating System (DOS), and UNIX. The recent trend is more towards UNIX, hence more and more CAD systems are offering both UNIX as well as DOS option. More and more workstations and PCs now adopt architectures, which allow them to run on almost all CAD systems.

### 5.6 **IDEAS (Integrated Design Engineering Analysis System):**

IDEAS is an integrated package of Mechanical Engineering software tools to help facilitate a concurrent engineering approach to Mechanical Engineering Product Design. I-DEAS allows the different groups in a Company to access the same data and exchange information freely.

IDEAS is made up of a number of "families" of products, each subdivided further into "modules" all executed from a common menu, and sharing a common database. (A module equals one computer executable program). The main families are Solid Modeling, Engineering Analysis, System Dynamics, Test Data Analysis, Drafting and Manufacturing.

### 5.7 **Solid Modeling:**

Solid Modeling contains the modules of Object Modeling and System Assembly. Together they are referred to as "Geomod". Object Modeling is the place where the geometry is actually defined. Geometry is represented as a solid, as

contrasted with surface or wire frame model programs. The created geometry can be used for mass and inertia property calculation, interference studies, Finite Element Modeling, Manufacturing.

To create a geometry the simplest method is to use primitive shapes such as blocks, cylinders, cones and spheres. More complex shapes can be made by extruding and revolving profiles. Use of skinning operation is done for complex structures which forms surfaces between different profiles. Joining or cutting objects is done using an object boolean operation.

System Assembly module allows building complex systems out of objects defined in Object Modeling. These systems can be used for visualization, mass properties calculation, interference studies.

#### 5.8 **Engineering Analysis:**

Engineering Analysis family is used to convert geometry into a Finite Element Model which in turn is used to analyze the effects of structural and thermal loads. The Pre/Post module is used to create the model and define the loads. The Model solution is then used to calculate the results from static, thermal or normal nodes analysis, which are redisplayed in the Pre/Post module.

Geometry created in Object Modeling can be used directly in Engineering Analysis or geometry can be created directly in Engineering Analysis. For sculptured surfaces or complex intersection of surfaces it is preferable to generate the geometry in Object Modeling.

Optimization module can be used to run several iterations to optimize a design to find optimum thickness parameters to minimize the weight, given various load cases.

#### 5.9 **System Dynamics:**

For those problems that require vibration analysis, I-DEAS system dynamics can be used to perform linear vibration analysis on dynamic system module. Vibration can be studied in the time domain (transition analysis) or in frequency domain.

#### 5.10 **Test Data Analysis:**

The goal in the Mechanical Computer Aided Engineering (MCAE) design process is to use testing through developmental cycle, and to make better use of the test data through more advanced analyses techniques and better integration with other disciplines. Initial test might be done on a prototype or previous design to understand the load environment and to develop loads for a finite element model.

Emphasis in IDEAS test data analysis is to make graphic representations of the numeric results in the form of 2D or 3D plots in various wire, bar or surface displays, or to display information directly on the geometry of the structure being tested.

## 5.11 **Methodology:**

In order to analyze the two plates, the IDEAS software package is used. First we have to make a solid model in the Solid Modeling Task. The shape of the





plate makes it difficult for us to make one complete solid model. Hence, we have to determine a way to divide the model into different parts. Because of the complex shape of the plate we divide the plate into three different parts. We store each part seperately, and later use the *JOIN* task to construct a solid model of the 135 and 150 degree plate.

The stem which is the first part is made by the "skinning" operation of two profiles. The end or the third part of the plate is created by extruding the profile in the Z-direction. The second or the middle portion of the plate is cylindrical and is joined with the end part by the "Boolean Join" operation. Finally the complete solid model is constructed by joining the two sub-parts. The joined second and third part is then bent at the desired angle. Holes are created in the stem using the Boolean cut operation.

We have to check for various errors like interference, overlapping geometry, etc. As soon as the solid model is created, it is ready for finite element analysis.

We go to the Finite Element Analysis Task and get the object from the stored object menu. Having recalled the object from the stored Solid Modeling Menu, we first create the Mesh areas for the plate. If there are any errors like incomplete loop, etc. we correct the errors. If we are able to create a complete mesh area for the various curves, our model is then ready to undergo transformation to one solid volume or various volumes. This is done to enable the software to generate nodes and elements in the Mesh Generation Task of the Finite Element

Analysis Menu.

Once the mesh volume/volumes are created either manually or automatically, we go to Mesh Generation Menu and pick the Solids Menu from it to generate nodes and elements for the Mesh volume. Having generated the nodes and elements, we store the nodes and elements. The list shows us exactly how many nodes and elements are generated and stored.

Having created the nodes and elements we write the workset to the ANSYS universal file. Using the ANSYS package we define the constraints, the nodes at which the forces will act. Once loading is done we check for any errors that might occur because of overlapping nodes and elements. We then generate the output file where we determine the values for nodal forces, displacements, shear stresses at the constraints and various nodes and elements.

# CAD SOFTWARE FEATURES AND ANALYSIS

# 5.12 2-D CAD Software:

Such software, is generally called drafting software, is most popular in industry due to the drafting capability, low cost and less demanding hardware requirements. It accounts for a major portion of the total CAD market.

There are four essential functions required by any drafting software. These are geometry creation, geometry editing, dimensioning and labeling, and input as well as output on peripherals. Geometry creation is the construction of a shape on the screen, using a set of standard elements which generally include points, lines,

arcs, circles, polygons etc. Generally, under "Draw" option, users are provided different options. Users are also able to insert the text in the design. For editing the geometry, the software provides basic options like "Erase" or "Remove" alongwith various options for visualization of the geometry like scaling to smaller image or bigger image, rotation in the 2-D plane, copying option, option for transalation of geometry, etc.

While editing the geometry the software should allow the user to edit part of the object by providing options like "Explode" or "Divide", which divides the geometry into a number of parts and then the user can edit the part required by the design. Also the software should provide the option for enclosing the required area of a drawing for translation or rotation of a group of lines, points or polygons. Also, options for filleting, chamfering, trimming should be provided to generate the design more precisely. For ease of creation of geometry, the software should have such options as "Orthogonal lines", "Reference Axis", "Grid layout", etc.

Dimensioning and labeling are also very important features. Dimensioning should include the use of super and subscripted text along with inside and outside dimensioning techniques, depending upon the space availability. Also, software should have " auto-dimensioning" option for ease of dimensioning and precision of drawing. The software should provide all these facilities associated with dimensioning.

For input/output of generated drawings the software should support dif-

ferent digitizers, mouse, keyboard, printers, plotters, etc. which are commonly available in the market.

# 5.13 **3-D CAD Software:**

Such software deals with three dimensional objects with side-view details of it. To deal with complex geometry and the inertial and sectional properties, such software uses various modeling methods.

A. *3-D Modeling Methods:* 

There are various methods for 3D modeling of an object. All 3D softwares use some of these methods to arrive at 3D modeling of any design. Following is a list of the modeling methods.

- (i) Wireframe Modeling
- (ii) Surface Modeling
- (iii) Solid Modeling
	- [a] Instancing scheme
	- [b] Spatial Occupancy Enumeration Scheme
	- [c] Cell decompostion scheme
	- [d] Sweep method
	- [e] Constructive Sold Geometry
	- [f] Boundary representation scheme
	- [g] Hybrid scheme

#### B. *Essential requirements of a 3-D Software:*

The basic capabilities of a 3-D software includes:

(i) An option to create a 3-D geometry with various techniques

(ii) An option to edit the created geometry and check the physical properties

(iii) An option for file utilities.

#### 5.14 **Hardware Support for 2-D and 3-D CAD Software:**

#### a. Memory Devices:

Memory devices are needed for the software to reside and to store the work done on the system. There are two type of memory devices. Primary storage devices are used for two type of memory, Random Access Memory (RAM) and Read Only Memory (ROM). ROM is used for storage of an Operating System. The part of RAM is used for storage of an application program, and the remaining portion of RAM is available for the user to store his work on the system. The size of memory referred in the commercial market is RAM.

The secondary storage can be thought in terms of disk drives. With the help of these drives, user can increase the memory storage capacity, in the range of 16K bytes to 1M bytes. With the help of a secondary storage, user can work with the complex CAD software package. The access time will be high and so the speed at which different operations are performed will be low.
Hardware used in SUN Micro Lab:



Some of the available tools of Sunview include:

Command Tool

Shell Tool

Text Editor - Font Editor

Icon Editor

Mail Tool

Debug Editor

Clock

Lockscreen

#### b. Input Devices:

#### [i] Digitizer

[ii] Mice

#### 5.15 **ANALYSIS SOFTWARE:**

The analysis software is used to test various stresses, strains, loads, etc. before it is put into operation. The conventional method of analysis is restricted to mathematical formula and the data available from that. With the development of CAD techniques, conventional analysis is replaced by an on screen analysis of component through various stress-strain criterion, and the sophisticated output results in terms of the different levels of loads, stress, strain, etc.

There are many analysis software available in the market. These are Finite element analysis (FEA), Dynamic analysis, Mechanism analysis, etc. The most popular analysis software is finite element analysis software. Since the work done in the thesis is related to FEA, we shall restrict the discussion in this section to finite element analysis software.

#### 5.15.1 **Capabilities of an FEA Software:**

The finite element analysis is based on arrays of large matrix equations that can only be realistically solved by a computer. Most often FEA is performed with commercial programs.

The finite element method is applicable in several types of analysis. The most common is static analysis, which solves for deflections, strain and stresses in structure under a constant set of applied loads. In most of the cases the material of a designed part is assumed to be linear elastic, but nonlinear behavior such as plastic deformation, creep and large deflections can also be analyzed.

Heat-transfer analysis can solve steady state and transient heat transfer problems. In most cases, the thermal output data are applied as an input to the structural analysis problem to determine thermal deflections and stresses.

The natural frequency analysis calculates the free vibration natural frequencies and associated mode shapes of a structure. This analysis used to predict the critical operating conditions for the machines.

The transient-dynamic analysis determines the time response history of a structure, subjected to a forced displacement function. Here the structure may behave linearly or in some cases friction, plasticity, large deflection or gaps may produce nonlinear behavior.

### 5.15.2 **General Structure of an FEA Software:**

All most all FEA Software are made up of three modules. These modules are Preprocessor, Model Solution and Postprocessor.

In preprocessor module, user can define the geometry and construct the mesh by defining the nodes, elements and surfaces. Most of the preprocessors ostensibly free the user of many routines, or otherwise time consuming tasks in constructing the mesh by offering the options such as automatic mesh generation, mesh copying, element reflection, etc. Accuracy of the mesh generation depends

on the type of geometry used for the basic construction. The time required in mesh generation depends on the type of geometry, number of elements and the processing speed of a computer. Generally, finer the mesh, more accurate the result of the analysis. After mesh generation, the model is defined with the actual load conditions.

Once the geometry is defined with the mesh and load conditions, the model is submitted to the model solution module. Depending on the software used, this module will solve the model with different techniques. Modern FEA software provides an option for the user to choose third party's solution module for the fast and accurate results.

The postprocessor module simplifies the interpretation of results by displaying the output data graphically. In case of conventional method, the results of analysis appears in the tabular form without any graphics. The output display may be in the form of contour stress plots, deformed geometry with undeformed geometry on it.



Fig. 13 Classification of screw position in femoral head

## CHAPTER VI

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### **CONCLUSIONS**

The placement of the fixation device in the subarticular region of the femoral head provides the most satisfactory hold. It has been proved that a nail parallel to the main weight-bearing seams in the femoral neck, provides the best protection against movement of the screw within the neck. The stability of the comminuted fracture is dependent on its ability to impact, without causing the screw to break or cut out. There are three positions (Fig. 11) which are very important for the right placement of the screw.

- 1. The center of the screw tip lying on the center line of the femoral head or within half the diameter of the screw from it.
- 2. The center of the screw tip lying between half a screw diameter and one screw diameter from the center of the head.
- 3. The center of the screw tip lying more than one screw diameter from the centerline of the femoral head.

The depth of penetration is evaluated by the distance of the end of the screw from the articular surface of the femoral head, as measured by the number of screw turns necessary before penetration of the joint would have occured. The

screw normally advances by 1/8th of an inch on every turn. The third position is invariably associated with subsequent movement of the screw within the head. In positions 1 and 2 the screws with a penetration of  $1/2$  an inch never moved. In the anteroposterior plane(position 3), alongwith position 2 in the lateral plane possibly allowed movement but no screw cut out. This clearly indicates how critical it is for the proper placement of the fixation device. If the screw is incorrectly placed, suitable precautions against undue stress should be taken after placement. Weight bearing on the fracture should be discouraged until union has occured. Repeated attempts at achieving perfect screw placement can lead to serious medical complications.

Placement of the 150° plate is difficult to achieve than the 135° plate because of its high angle. The 150° plate occupies a rather high position in the head, and since it enters the shaft below the fracture site in rather thick cortical bone, the angle of entry has to be exact. The bone in the cortical region is too thick to permit any crushing, to correct minor errors of the angle of insertion, hence for routine purposes a 135° plate is recommended. The 150° plate should be used in those fractures, in which the lesser trochanter calcar fragment is so large, that considerable medial displacement and shortening are necessary to achieve stability. The 150° plate in this position allows the fracture to be placed in valgus, the screw entering the proximal fragments, through the open medulary cavity, and being correctly placed centrally within the head. This valgus position compensates for the inevitable shortening. Despite the theoretical mechanical advantages associated with a 150° plate, the 135° proves easier to use and allows impaction well.

Solving the simultaneous equations by using the *Mathematica* software package the values of the unknown variables like the reaction forces **R1, R2, R3,**   $R_4$ ,  $X_4$ ,  $\sigma_{calc.}$ , etc. can be found. Varying the values of these different variables alters the value of stress. The results from the Mathematical Model indicate that the 150° plate is superior from the mechanical point of view because of the high angle and strength.

Using the FEM Model we are able to conclude that the assumptions made in the mathematical model hold true. Using the ANSYS software package we are able to calculate the value of stresses and displacements at various nodes and elements in the two plates. The values calculated for the first hole for the 135 degree plate are as follows:

$$
\sigma_x = 2.473N/mm^2
$$
,  $\sigma_y = 0.78433N/mm^2$  and  $\sigma_z = 0.20139N/mm^2$ .

The displacement at the first hole  $U_x$ ,  $U_y$  and  $U_z$  are equal to zero, since the constraints are applied at the holes.

Similarly the values calculated for the 150 degree plate are:

$$
\sigma_x
$$
 = 0.172595*N/mm*<sup>2</sup>,  $\sigma_y$  = -0.412328*E* - 01*N/mm*<sup>2</sup> and  $\sigma_z$  = -0.306374*N/mm*<sup>2</sup>,

displacements  $U_x$ ,  $U_y$  and  $U_z=0$ . From the results we can conclude that from the engineering point of view the 150 degree plate has lower stress values at the constraints, and is superior to the 135 degree plate. It is then recommended to use a compromise angle between 135° and 150° plate to have lower stresses and to ease the method of plate insertion.



Fig. 14. Plot of  $\sigma_x$  v/s 'X' for 135 ° plate

 $\sigma_x$  v/s X<br>For 135° plate

 $\sigma_z$  v/s X<br>For 150° plate



Fig. 15. Plot of  $\sigma_x$  v/s 'X' for 150 ° plate

### CHAPTER **VII**

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# **Comparative Study of Failures in different Plates**



## **TABLE <sup>122</sup>**



 $\sim 10^{-1}$ 

 $\mathcal{L}^{(1)}$ 

 $\sim 10^{-1}$ 







### **Proportion of Elements in S.S. Nails**



# TABLE II<sup>22</sup>





TABLE III46